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Representation of Quasi-Biennial Oscillation in JRA-3Q

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Abstract

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This study evaluates the representation of the quasi-biennial oscillation (QBO) in zonal

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wind and temperature in Japanese Reanalysis of Three Quarters of a Century (JRA-3Q).

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We examine the temporal consistency of the QBO between the post- and pre-satellite

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eras, by comparing it with other reanalyses and observations of radiosonde and satellite

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data. Here, we quantify the disagreement between the post- and pre-satellite eras using

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the background spectrum based on the post-satellite era. In the satellite era, the QBO

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amplitudes of the zonal wind and temperature at 20–30 hPa are somewhat reduced in

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JRA-3Q by approximately 8% and 4%, respectively, compared with other reanalyses.

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However, the JRA-3Q QBO from the early 1960s and before is substantially degraded,

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falling below the 95% confidence level. The representation of the JRA-3Q annual

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oscillation in the equatorial stratosphere is improved, whereas that in the pre-satellite era

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in the Japanese 55-year Reanalysis completely disappears due to unrealistically strong

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damping. The zonal asymmetry of the zonal wind QBO amplitude is characterized by a

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wave-1 structure with a magnitude of approximately 1 m s^{-1} in the middle-to-upper

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stratosphere and a larger amplitude in the central Pacific in the lower stratosphere,

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consistent with previous studies. The disconnection of temperature QBO-amplitude

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anomalies between the lower and middle stratosphere is observed in some reanalyses,

41 whereas those in JRA-3Q exhibit an eastward tilt with height, although underlying cause
42 of these anomalies remains unclear.

43 In short, QBOs remain a challenge especially with high-resolution models. 1) How to
44 tune the high-resolution-version QBOs to match lower-resolution versions set up for
45 climate when restricted to outputs over the short numerical weather prediction timescales.
46 2) How to sustain QBO amplitudes further into the past with limited data availability. This
47 study has a broader applicability than simply development of reanalysis systems, and
48 understanding and implications of their limitations.

49

50 **Keywords** reanalysis; quasi-biennial oscillation; wavelet analysis; JRA-3Q;

52 **1. Introduction**

53 The dominant mode of variability in the tropical lower-to-mid stratosphere is the quasi-
54 biennial oscillation (QBO), which is approximately zonally symmetric and is characterized
55 by alternating westerly and easterly phases propagating downward in the equatorial
56 stratosphere with a frequency of 2–3 years (Baldwin et al. 2001; Anstey et al. 2022b). The
57 QBO significantly influences the entire stratosphere and even the troposphere through the
58 troposphere-stratosphere coupling. In the tropical upper stratosphere, the semi-annual-
59 oscillation (SAO) (e.g., Ern et al. 2021) and annual oscillation (ANN) are dominant, although
60 a small component of QBO variability extends into the upper stratosphere and mesosphere.

61 The reanalysis integrates model data with observations worldwide to produce a high-
62 quality climate dataset using a consistent, state-of-the-art data assimilation system. Modern
63 reanalyses significantly contribute to the verification of phenomena such as the QBO.
64 According to a comparison of reanalyses by Randel et al. (2004), significant differences
65 were documented in the representation of the stratosphere among different analyses.
66 Subsequent, continuous improvements in reanalyses led to considerably smaller differences
67 in QBO representation among modern reanalyses (Kawatani et al. 2016). Recently, the
68 Stratosphere–troposphere Processes And their Role in Climate (SPARC) (2022) conducted
69 a coordinated intercomparison of reanalysis data sets, focusing on key diagnostics including
70 the QBO, and it aimed at elucidating the underlying cause of these discrepancies. Wind
71 profiles from tropical radiosonde stations constitutes the primary observational constraint for

72 the QBO in the reanalysis, whereas the global coverage provided by satellite observations
73 since the late 1970s has some impacts on the tropical stratosphere (Anstey et al. 2022a).
74 Thus, it is interesting to assess the reliability of QBO representation in the state-of-the-art
75 reanalysis for the pre-satellite era and to evaluate the extent to which the modern reanalysis
76 realistically captures QBO by comparing it with independent observations. This evaluation
77 is crucial for remaining issues among reanalyses.

78 Modeling studies employing general circulation models (GCMs), have attempted to
79 realistically simulate the QBO. Takahashi (1996) first simulated QBO-like oscillations with a
80 1.5-year period using a GCM with a spectral truncation of T21 and 60 vertical layers. This
81 model utilized a vertical resolution of 500 m in the upper troposphere and lower stratosphere,
82 along with reduced horizontal diffusion in those regions. Subsequently, QBO-like oscillations
83 have been produced in many models (e.g., Hamilton et al. 1999; Scaife et al. 2000; Giorgetta
84 et al. 2002; Shibata and Deushi 2005). Watanabe et al. (2008) demonstrated a spontaneous
85 QBO-like oscillation in their simulations without employing parameterizations for gravity
86 wave drag (GWD). Instead, they incorporated convection, topography, instability, and
87 adjustment processes. There were three modifications to facilitate the development of QBO-
88 like oscillations in general circulation and chemistry-climate models (e.g., Shibata and
89 Deushi 2005; Takahashi 1996): 1) employing fine vertical layers in the upper troposphere
90 and stratosphere, 2) reducing horizontal diffusion further below standard values in the
91 stratosphere and above, and 3) replacing the Rayleigh friction used in earlier versions by

92 introducing the nonorographic GWD scheme proposed by Hines (1997).

93 Over two decades after the first simulated QBO-like oscillation, significant uncertainty
94 remains regarding the requirements for achieving a QBO in free-running atmospheric GCMs
95 and Earth system models (ESMs) without data assimilation. These models depend on
96 parameterized nonorographic GWD, often tuned to improve model performance in the
97 stratosphere and mesosphere, including the QBO, and to provide much of the QBO wave
98 forcing. To improve the simulation of tropical stratospheric variability in GCMs/ESMs, the
99 SPARC/QBO initiative (QBOi) conducted a series of coordinated experiments (Butchart et
100 al. 2018). They found that free-running models may either underestimate or overestimate
101 the QBO amplitude and exhibit significantly larger quantitative and qualitative discrepancies
102 in their representation of the QBO compared to various reanalyses (Bushell et al. 2022;
103 Schenzinger et al. 2017). This implies that even with high-resolution models accurately
104 simulating a realistic QBO is still challenging.

105 Until recently, specifically before the 2010s, a nonorographic GWD parametrization was
106 incorporated into several reanalysis models including the Climate Forecast System version
107 2 (CFSv2; Saha et al. 2014), European Centre for Medium-Range Weather Forecasts
108 (ECMWF) 20th century reanalysis (ERA-20C; Poli. 2016), and the Modern-Era
109 Retrospective Analysis for Research and Applications (MERRA; Rienecker et al. 2011).
110 These reanalyses managed to resolve the impacts of small-scale contribution from gravity
111 waves (Table 2.7 of SPARC 2022, which summarized GWD parameterizations used in the

112 forecast models of the reanalysis). However, introducing a nonorographic GWD
113 parametrization did not guarantee the generation of a realistic QBO (Anstey et al. 2022a).
114 This means that especially with high-resolution models, reanalysis QBOs remain a
115 challenge as we have yet to solve the problem of tuning over the short numerical weather
116 prediction (NWP) timescales that we can afford to run, but the goal is accurate prediction of
117 oscillation characteristics that can only be evaluated after many years of simulation (or
118 analysis).

119 The first reanalysis QBO represented realistically using a self-generated QBO in a
120 forecast model was MERRA version 2 (MERRA-2; Gelaro et al. 2017), which improved the
121 representation of QBO forcings by adopting a parameterized GWD scheme (Coy et al. 2016).
122 While the GWD parameterization in MERRA-2 was similar to that in MERRA, the latitudinal
123 profile of the background nonorographic GWD in the MERRA-2 was modified to include a
124 source related to tropical and storm-track precipitation (Molod et al. 2015). The increased
125 equatorial GWD in MERRA-2 reduced the zonal wind analysis increments compared with
126 MERRA, thereby making the QBO mean meridional circulation more physically consistent
127 (Coy et al. 2016). However, this GWD parameterization do not always contribute to the entire
128 range of QBO characteristics in the equatorial stratosphere. For instance, the SAO is notably
129 stronger at 5 hPa and above (Coy et al. 2016; Shibata and Naoe 2025). The QBO winds at
130 10 hPa were a clear outlier during the period before the mid-1990s, which would be
131 attributed to the downward propagation of exceptionally strong westerly SAO phases in the

132 reanalysis (Kawatani et al. 2016; Anstey et al. 2022a).

133 The second reanalysis QBO represented realistically using a self-generated QBO was
134 the fifth generation ECMWF reanalysis (ERA5). ERA5 introduced the nonorographic GWD
135 parametrization of the Scinocca (2003) scheme to represent the effects of upward
136 propagating gravity waves from tropospheric sources including deep convection, frontal
137 disturbances, and shear zones (Orr et al. 2010; Hersbach et al. 2020; Pahlavan et al. 2021a,
138 b). The GWD parameterization in ERA5 was the same as ERA-20C, except for incorporating
139 a latitudinal dependency of nonorographic launch flux. Using the parameterization in a free-
140 running model run yielded a QBO-like oscillation with relatively realistic amplitudes. However,
141 the period of these oscillations was approximately 1.2 years, which was notably shorter than
142 the observed QBO (Orr et al. 2010).

143 The Japanese Reanalysis of Three Quarters of a Century (JRA-3Q) is the latest third
144 generation of global atmospheric reanalysis spanning late 1940s onward (Kosaka et al.
145 2024). JRA-3Q used a scheme proposed by Scinocca (2003), which parameterized the
146 momentum-conserving vertical propagation and dissipation processes of momentum. The
147 dissipation processes were represented through critical-level filtering and amplitude
148 saturation (Japan Meteorological Agency 2019). This scheme is more advanced than that
149 in JRA-55 (S. Kobayashi et al. 2015), which only employed Rayleigh friction for layers above
150 50 hPa (Japan Meteorological Agency 2013).

151 Typical questions arise regarding the representation of the JRA-3Q QBO. How well does

152 JRA-3Q representation of the QBO align with other datasets? To what extent can we
153 quantify differences in the representation of the QBO among reanalyses and observations?
154 Is it appropriate to use reanalysis data from the pre-satellite era? Are there specific aspects
155 of the JRA-3Q QBO that should be considered when using it? Because globally
156 comprehensive observational datasets are not available during the pre-satellite era, the
157 JRA-3Q QBO is evaluated by comparisons with other reanalyses and observations, as well
158 as through comparisons between the post-satellite and pre-satellite eras. This study is
159 conducted to evaluate the representation of JRA-3Q QBO in zonal wind and temperature,
160 with an emphasis on maintaining consistency over time in the reanalysis QBO.

161 The structure of this paper is as follows. Section 2 describes the QBO in the JRA-3Q
162 system and the methods used to isolate the QBO signal in the reanalysis. Section 3
163 characterizes the morphology of the QBO. In Section 4, we present results illustrating the
164 QBO signal through the wavelet analysis, including trends in amplitude and period, as well
165 as the latitudinal structure and longitudinal asymmetry derived from the wavelet analysis.
166 Finally, Section 5 provides discussion and conclusions.

167

168 **2. Data and Method**

169 2.1 Datasets

170 Monthly mean zonal wind values, which are representative of the equatorial belt, are
171 analyzed using data from global reanalysis datasets, including JRA-3Q, ERA5, MERRA-2,
172 and JRA-55, along with JRA-55C (C. Kobayashi et al. 2014).

173 A long-term combined radiosonde dataset, compiled by the Free University of Berlin
174 (FUB; Naujokat 1986) (<https://www.geo.fu-berlin.de/en/met/ag/strat/produkte/qbo/index.html>), is utilized near the equator at three
175 stations: Canton Island (2.8°S, 171.7°W); Gan, Maldives (0.7°S, 73.1°E); and Singapore
176 (1.4°N, 103.9°E) at the 70, 50, 40, 30, 20, 15 and 10 hPa levels from 1953 to 2020. Additional
177 Singapore sonde data were obtained from a National Aeronautics and Space Administration
178 (NASA) site (https://acd-ext.gsfc.nasa.gov/Data_services/met/qbo/qbo.html), covering the
179 period from 1979 to the present. In this study, we construct a merged dataset combining the
180 FUB data from 1953–2020 and the NASA data from 2021–2023. Hereafter, these merged
181 data are referred to as radiosonde data (or sonde observations). For satellite observation
182 data, we utilized temperatures measured by the Microwave Limb Sounder (MLS) instrument
183 on the Aura satellite (AMLS), along with winds derived from the AMLS geopotential height
184 data (Shibata and Naoe 2025). Both the AMLS temperature and geopotential height data
185 were obtained from Level 3 monthly binned datasets, version 5.0x (Livesey et al. 2022), with
186 a latitudinal resolution of 4.0 degrees (available online from

188 https://acdisc.gesdisc.eosdis.nasa.gov/data/Aura_MLS_Level3/). These datasets, spanning
189 from 2004 to 2022, are available at Aura MLS Level 3 data. The zonal wind outside the
190 equatorial area was calculated from the geopotential height data using the gradient wind
191 balance equation. In the vicinity of the equator, zonal wind was evaluated through cubic
192 spline interpolation of the gradient wind outside the near-equator latitudes, following the
193 method described by Smith et al. (2017). More detailed explanations were described by
194 Shibata and Naoe (2025).

195

196 2.2 Wavelet analysis

197 The wavelet analysis provides a measure of the dominant time-dependent modes of
198 variability by decomposing a time series in the time-frequency domain. This technique is
199 applied to the QBO analyses (Fadnavis and Beig 2008; Naoe et al. 2017; Shibata and Naoe
200 2022). In this study, a Morlet mother wavelet, a plane wave modified by a Gaussian envelope,
201 with a nondimensional frequency $\omega_0 = 6$ (e.g., Torrence and Compo 1998) is used. To
202 examine fluctuations in the QBO power over a range of scale (or bands), the scale-averaged
203 wavelet power P_{QBO} at a given time index is calculated. This measure represents a time
204 series of the average variance within a specific band, derived from the weighted sum of the
205 wavelet power spectrum within a band from 20 to 40 months. The QBO amplitude is
206 evaluated as the square root of $2P_{QBO}$. Thus, the scale-averaged wavelet power can be
207 used to examine the modulation of one time series by another, or the modulation of one

208 frequency by another within the same time series.

209 Based on Torrence and Compo (1998), we derive the significance (or confidence level)
 210 for Fourier and wavelet spectra. A background spectrum of red noise can be modelled as a
 211 lag-1 autoregressive [AR(1)] process. The discrete Fourier power spectrum (Gilman et al.
 212 1963) with the assumed AR(1) α is given by

$$213 \quad P_k = \frac{1-\alpha^2}{1+\alpha^2-2\alpha \cos(2\pi k/N)}, \quad (1)$$

214 where $k = 1 \cdots N/2$ is the frequency index. On average, the local wavelet power spectrum is
 215 identical to the Fourier power spectrum given by Eq. (1) (Torrence and Compo 1998).

216 The null hypothesis for the wavelet power is defined such that if a peak in the wavelet
 217 power spectrum significantly exceeds the background spectrum, then it can be considered
 218 a true feature with a specified level of confidence (e.g., at the 95% confidence level, or
 219 equivalently significant at the 5% level). If the wavelet coefficient follows a normal distribution,
 220 then both the real and imaginary parts of the wavelet coefficient are also normally distributed.
 221 As the square of a normally distributed variable is chi-square distributed with one degree of
 222 freedom (DOF), the wavelet power spectrum should be normally distributed with two DOF,
 223 denoted by χ_2^2 . Assuming a mean background spectrum of red noise as described by Eq.
 224 (1), the corresponding distribution for the local wavelet power spectrum, $|W_n(s)|^2$, is given
 225 by

$$226 \quad \frac{|W_n(s)|^2}{\sigma^2} \Rightarrow \frac{1}{2} P_k \chi_2^2 \quad (2)$$

227 at each time n and wavelet scale s , where σ^2 is the variance and “ \Rightarrow ” indicates “is

228 distributed as". Thus, by selecting an appropriate AR(1), Eq. (2) can be calculated at each
229 scale to construct 95% confidence levels.

230 By smoothing the wavelet spectrum in time, one can increase the DOF of each point and
231 increase the significance of peaks in wavelet power (Appendix). Additionally, smoothing in
232 scale increases the DOF, and thus an analytical relationship for significance levels for the
233 scale-averaged wavelet power is described in Appendix.

234 The QBO amplitude is calculated by two independent methods: the direct method and
235 the wavelet method (Shibata and Deushi 2012; Shibata and Naoe 2022). For the direct
236 method, the QBO time series assumes a single sinusoidal wave (Pascoe et al. 2005;
237 Baldwin and Gray 2005), for example, $A \sin(t)$. As the peak value is A and the variance is
238 $A^2/2$, the QBO amplitude is $\sqrt{2}\sigma$, where σ is the root mean square of the QBO time series
239 over three cycles. The $\sqrt{2}$ factor is used to make the defined amplitude representative of
240 the magnitude of the peak of the oscillation (Dunkerton and Delisi 1985). As described by
241 Shibata and Naoe (2022), one cycle is defined as the period from one minimum point of the
242 magnitude of the QBO time series to the second consecutive minimum point. The QBO
243 amplitude is assigned to the center time of the three cycles. In this way, the QBO amplitudes
244 are first calculated discretely in time, approximately half a cycle (~14 months) apart. Monthly
245 amplitudes are then obtained through cubic interpolation using Lagrange polynomials.
246 Henceforth, this direct method is referred to as a sigma method.

247

248 **3. Representation of QBOs in Reanalyses**

249 3.1 QBO Time Series and Spectrum

250 Figure 1 presents the time series of zonal-mean zonal wind at the equator for reanalysis
251 datasets including JRA-3Q, JRA-55, ERA5 and MERRA-2, alongside observations from
252 AMLS and radiosondes at Singapore or other near-equator stations. Overall, analyses
253 QBOs are in good agreement with the radiosonde observations in the post-satellite era,
254 illustrating the basic-features of the zonally-averaged QBO. The zonal winds alternate
255 between westerly and easterly phases with variable durations. Generally, westerly QBO
256 phases tend to persist longer at lower levels, while easterly phases dominate at higher levels.
257 The westerly QBO phases have roughly constant amplitude with height while easterly QBO
258 phases tend to be strengthened with increasing height (e.g., Baldwin et al. 2001; Anstey et
259 al. 2022a). QBO disruptions, such as intrusions near 40 hPa followed by the descent of
260 easterly anomalies within a westerly QBO phase, are evident (Newmann et al. 2016; Osprey
261 et al. 2016; Coy et al. 2017). In the post-satellite era, the JRA-3Q QBO appears consistent
262 with that in JRA-55. The MERRA-2 QBO winds, especially the westerly winds, appear
263 slightly stronger, and the SAO is notably stronger at 5 hPa and above (Coy et al. 2016).
264 Additionally, westerly onsets in MERRA-2 tend to occur earlier than westerly onsets (Anstey
265 et al. 2022a) in the other three reanalyses.

266 In the pre-satellite era, deviations between the JRA-3Q QBO and radiosonde
267 observations appear in the 1970s, showing an easterly shift in the 1960s and diminished

268 QBO signals in the 1950s. Meanwhile, the JRA-55 QBO during the 1960s exhibits similar
269 characteristics to ERA5. The ERA5 QBO shows a behavior consistent with observations in
270 the lower stratosphere dating back to the mid-1950s. The JRA-3Q QBO in its early stage
271 exhibits a shorter period of around one year in the middle stratosphere and a diminished
272 amplitude in the lower stratosphere before the late 1960s. Therefore, the modelled QBO in
273 JRA-3Q has a lack of consistency with the observed QBO, and the representation of the
274 assimilated QBO in JRA-3Q only with conventional observations is not good as that in JRA-
275 55. It is noteworthy that while the JRA-3Q model can produce a self-generated-QBO, the
276 atmospheric model in JRA-55 did not produce any QBO-like oscillations (Kosaka et al. 2024).

277 Figure 2 displays the power spectrum of zonal-mean zonal wind at the equator spanning
278 20 years of both post-satellite and pre-satellite eras. Three primary components are evident:
279 a narrow spectrum of the SAO and ANN above approximately 5 hPa, with power peaks at 1
280 hPa and around 2 hPa, respectively, and a broad QBO spectrum between 2 and 3 years
281 which does not overlap with the other components. For this study, QBO components are
282 defined as oscillations with periods ranging from 20 to 40 months, consistent with previous
283 studies (Pascoe et al. 2005; Shibata and Naoe 2022). As the QBO power peaks at
284 approximately 20 hPa (Fig. 2), the characteristics of the QBO are primarily investigated at
285 this altitude. The zonal wind QBO clearly dominates the wind variability in the middle
286 stratosphere, while the temperature peaks slightly below the wind peak, with temperature
287 variations observed above the tropical tropopause (Supplement Figure S1).

288 In pre-satellite era, JRA-3Q does not reproduce QBO well, exhibiting unrealistic false
289 peaks at 9 and 18 months. Conversely, the SAO and ANN show a relatively good agreement
290 with those in the post-satellite era. In contrast, JRA-55 effectively represents the QBO, but
291 it does not reproduce the ANN, with its power nearly diminished and only visible around 3–
292 5 hPa below the main ANN region. This discrepancy is likely attributed to stronger damping
293 in the upper layers of the atmospheric model to prevent reflections from the top lid.

294

295 3.2 Comparison of processes represented by reanalysis models

296 Here, we describe the representation of the QBO in zonal wind and temperature in JRA-
297 3Q compared to the JRA-55 QBO. Anstey et al. (2022a) indicated that the assimilation of
298 satellite observations does not necessarily have a significant impact on the representation
299 of QBO wind evolution. This finding was supported by the effective constraint of tropical
300 radiosonde wind observations up to altitudes of 10 hPa in JRA-55, as demonstrated by the
301 excellent agreement between JRA-55 and JRA-55C reanalyses (C. Kobayashi et al. 2014).

302 However, JRA-55 lacked the ability of its underlying model to self-generate its own QBO.
303 Additionally, it included unrealistically strong damping terms in the middle atmosphere,
304 leading to the disappearance of the ANN peak, typically observed at 2 hPa, during the pre-
305 satellite era (Fig. 2). To mitigate the accumulation of smallest-scale noise, JRA-55 employed
306 fourth-order linear horizontal diffusion of vorticity and divergence on spectral variables in
307 terms of spherical harmonics (Japan Meteorological Agency 2013). These diffusion

308 coefficients gradually increased with height in layers above 100 hPa, simulating a sponge
309 layer designed to absorb waves approaching the upper boundary. The Rayleigh friction was
310 also implemented for layers above 50 hPa. Vertical diffusion of momentum and heat were
311 represented by the surface boundary layer scheme from the Level 2 turbulence closure
312 scheme of Mellor and Yamada (1974) across the entire atmosphere (Japan Meteorological
313 Agency 2013).

314 JRA-3Q improved the representation of the forecast model by adopting the more
315 sophisticated, nonorographic GWD scheme compared to JRA-55 (Kosaka et al. 2024). The
316 model top was extended up to 0.01 hPa from 0.1 hPa, and the vertical resolution was
317 increased from 60 to 100 layers in JRA-3Q. To mitigate the accumulation of smallest-scale
318 noise, second-order linear horizontal diffusion was applied to the divergence term in
319 spherical harmonics. The diffusion coefficient progressively increased with height in a
320 sponge layer located above 30 hPa. Vertical diffusion of momentum and heat were
321 represented by the surface boundary layer scheme using a hybrid approach that combined
322 a turbulence kinetic energy closure scheme based on Mellor and Yamada (1974, 1982) with
323 an eddy diffusivity type scheme based on Han and Pan (2011) throughout the entire
324 atmosphere (Japan Meteorological Agency 2019). As a result, the JRA-3Q is capable of
325 reproducing ANN in the upper equatorial stratosphere during the pre-satellite era. The JRA-
326 3Q introduced the scheme developed by Scinocca (2003), using a launch level of 450 hPa
327 and launch momentum flux of 3.5 mPa. The Scinocca scheme is designed with simplicity;

328 once the properties of the launch spectrum are selected, the only tunable parameters in
329 practice are the launch level and total launch momentum flux (Orr et al. 2010).

330 Here, there is a frequently faced dilemma for developers of models for operational
331 weather prediction that lower resolution versions set up for climate simulations can be tuned
332 to represent QBO behaviors under present day conditions that are relatively realistic (albeit
333 imperfect) but the highest resolution versions are too expensive to run beyond the short
334 NWP, or at most seasonal, timescales. Thus, there are double challenges: 1) How to tune
335 the high-resolution versions of models to produce “free-running” QBOs that at least match
336 the realism of low-resolution models given output that is overwhelmingly on short timescales
337 heavily influenced by initial conditions. Reanalyses which cover historical periods may not
338 have sufficient observational data to constrain the model behavior, leading to divergence
339 between datasets prior to introduction of higher density observations. 2) How to be able to
340 sustain QBO amplitudes further into the past with limited data availability.

341 Due to that dilemma that parameters representing the QBO were not sufficiently tuned,
342 the JRA-3Q QBO exhibits a model bias when compared with observational data. In the
343 satellite era, the model bias was corrected by the availability of sufficient satellite
344 observations. However, in the pre-satellite era, the model bias was more pronounced due
345 to the sparse conventional observations available in the early stage of the historical timeline.
346 Consequently, the JRA-3Q QBO from the early 1960s and before has substantially different
347 characteristics from the QBO observed in the post-satellite era.

348

349 **4. QBO Characteristics Using the Wavelet Analysis**350 **4.1 Wavelet spectrum and scale averaged wavelet power amplitude**

351 Figure 3 depicts both local and global (or time-averaged) wavelet spectra of JRA-3Q
352 zonal-mean zonal wind at 20 hPa. The local wavelet spectrum is presented for January 2010,
353 while the time-averaged spectra span 21-years in both the post-satellite and pre-satellite
354 eras. These spectra are normalized by a variance value of approximately $300 \text{ m}^2 \text{ s}^{-2}$. A thin
355 gray line represents the mean red noise spectrum, which is a theoretical background noise
356 with a $\text{AR}(1)$ of 0.94. It is important to note that the variance and $\text{AR}(1)$ calculations are
357 based on deseasonalized and detrended zonal wind data exclusively from the post-satellite
358 era, primarily from 1980 to 2022. This background spectrum serves as a reference for
359 evaluating the QBO in the pre-satellite era as well. The upper thick gray line corresponds to
360 the 95% confidence spectrum, assuming that the square of a normally distributed variable
361 follows a chi-square distribution with two DOF (for each real and imaginary part of complex
362 wavelet transform function).

363 Color dashed (green, red, and blue) horizontal lines represent the sum of the wavelet
364 power spectrum between 20 and 40 months, scaled to estimate the QBO wavelet power
365 (Torrence and Compo 1998). Thick gray horizontal dashed lines indicate the scale-averaged
366 95% confidence level. The scaled-averaged power associated with the QBO exceeds the
367 95% level during the satellite era (red line), whereas QBO power in the pre-satellite era (blue

368 line) remains quite low and comparable to the 95% confidence level. Additionally, an
369 unrealistic spectrum with a period of 6–12 months, which is clearly a part of model bias, is
370 enhanced. This indicates that the representation of the JRA-3Q QBO in the early stage is
371 significantly degraded due to the outstanding model bias and this QBO does not dominate
372 variability in the equatorial middle stratosphere.

373 Figure 4 displays the time series of the wavelet power spectrum at 20 hPa for each
374 dataset. All datasets exhibit similar behavior with amplitude peaking around 28 months
375 within 20 to 40 months, remaining relatively constant throughout the satellite era. It appears
376 that during the 2010s, the QBO period lengthens, displaying greater variability likely due to
377 the QBO disruption observed in 2016 (Coy et al. 2017; Newmann et al. 2016; Osprey et al.
378 2016).

379 Figure 5 illustrates the time series of the vertical profile of wavelet power amplitude of
380 zonal wind at the equator for the reanalyses and observations. The QBO clearly dominates
381 the zonal wind variability in the 10–70 hPa layer, peaking around 20 hPa. It is noted that the
382 AMLS zonal wind at the equator is evaluated using AMLS monthly geopotential height data.
383 Therefore, the derived zonal wind serves as a rough estimation and is used qualitatively for
384 comparison with the reanalyses. Throughout its period, including the pre-satellite era, JRA-
385 55 QBO exhibits no significant long-term trend in the QBO amplitude, highlighting the
386 importance of conventional observations in accurately reproducing the QBO within the JRA-
387 55 reanalysis system (Anstey et al. 2022a). For JRA-3Q in the pre-satellite era and ERA5 in

388 its early stage, QBO amplitudes diminish rapidly above 10 hPa falling clearly below the 95%
389 confidence level in the post-satellite era. This suggests that no direct wind observations
390 were assimilated at these higher altitudes in these datasets.

391 Figure S2 shows the time series of the vertical profile for temperature. The temperature
392 QBO dominates variability in the 10–70 hPa layer, with amplitude ranging from 2–3 K and
393 peaking at 20–30 hPa. Both JRA-3Q and JRA-55 exhibit variations in temperature QBO
394 amplitudes at 5–10 hPa before and after 1998, possibly influenced by a significant transition
395 in satellite instruments from TOVS to ATOVS suites in 1998 (Kosaka et al. 2024). Kim et al.
396 (2019) identified systematic changes around 1998 in Kelvin wave amplitudes in JRA-55
397 compared with JRA-55C, suggesting impacts of different satellite data on assimilated
398 equatorial wave fields.

399 QBO amplitude is calculated using both the sigma method and wavelet method for JRA-
400 3Q. In the sigma method, one cycle is defined from the minimum points of the band-passed
401 data, as shown by star marks in Fig. 6. Meanwhile, in the wavelet method, fluctuations are
402 examined in power over a range of scales (or a band), and one can define the scale-
403 averaged QBO wavelet power as the weighted sum over scales from 20 to 40 months. This
404 scale-averaged wavelet power provides a time series of average variance within a specific
405 band, offering insights into the modulation of frequencies within the same time series.

406 Figure 6 illustrates the time series of the QBO amplitude of the zonal-mean zonal wind
407 at 20 hPa for JRA-3Q, calculated using both the sigma method and wavelet method,

408 alongside the magnitude of band-pass filtered zonal wind. Apparently, the QBO amplitude
409 closely tracks the envelope of the band-pass filtered zonal-mean zonal wind magnitude. The
410 sigma method exhibits decadal variations similar to the wavelet method but with less short-
411 period variability, indicating an effective filtering of shorter periods below a few years
412 (Shibata and Naoe 2022). The time series reveals consistent interdecadal changes,
413 including potential modulation in QBO variance with decadal oscillation and peaks in QBO
414 amplitude around the late 1960s, 1983, 1995, and 2005 (Hamilton 2002; Shibata and Naoe
415 2022), as well as the QBO disruption observed in the late 2010s (e.g., Coy et al. 2017). The
416 thin solid line represents the 95% confidence level for zonal wind (assuming red noise with
417 $\alpha = 0.93$), estimated from satellite era data spanning 1980–2022. Figure 7 compares the
418 zonal wind amplitude of the JRA-3Q QBO at 20 hPa with other reanalyses, and observations
419 from the radiosonde and AMLS. As sonde winds are sampled at specific locations, whereas
420 the other datasets show zonally-averaged winds, the sonde amplitude of zonal wind QBO
421 should not be considered an exact representation of the amplitude derived from reanalyses.
422 Overall, however, almost all reanalyses show good agreement with each other and with the
423 sonde data, and there is a marked convergence over the latest 15 years. In the 1982–2020
424 average, the QBO amplitude for the mean of the four reanalyses is 22.8 m s^{-1} , slightly lower
425 than the sonde amplitude of 25.0 m s^{-1} . In contrast, the AMLS QBO amplitude during 2007–
426 2020 underestimates the four reanalysis mean by 22%, although this value exceeds the
427 95% confidence level of the 4-reanalysis mean. Specifically, the JRA-3Q QBO amplitude

428 during the satellite era appears as somewhat of an outlier before the mid-2000s, reduced
429 by 8% compared with the other reanalyses.

430 In the pre-satellite era, the JRA-3Q QBO amplitude significantly deteriorates falling below
431 the 95% level in the early 1960s and before. The ERA5 QBO amplitude (and JRA-55 QBO
432 amplitude) exhibit behavior consistent with sonde observations, remaining above the 95%
433 confidence level as long as conventional sonde observational data are available. Prior to the
434 availability of radiosonde data, however, the ERA5 QBO amplitude also falls below the 95%
435 level.

436 Anstey et al. (2022a) suggested that differences in QBO representation between JRA-
437 55 and JRA-55C did not exhibit any long-term trend, indicating that the increasing
438 incorporation of satellite data into JRA-55 did not significantly improve QBO representation
439 compared to conventional observations alone. In the JRA-3Q data assimilation system, the
440 nonorographic GWD scheme was used for improving the representation of the QBO. These
441 results suggest that satellite data are important for correcting significant model biases in the
442 JRA-3Q data assimilation system. While the GWD scheme in JRA-3Q is beneficial, it does
443 not inherently guarantee the generation of a realistic QBO, particularly evident in the pre-
444 satellite era.

445 Comparing the zonal wind QBO to the temperature QBO, it is expected that the inter-
446 reanalysis spread of zonal wind is larger in the tropics than that of temperature due to the
447 weaker constraint provided by satellite-derived temperature observations. In Fig. 7b, it is

448 evident that the temperature QBO from AMLS shows a good agreement with those from the
449 reanalyses. The temperature QBOs exhibit amplitudes of 2–3 K at 30 hPa, with a mean
450 value of 2.3 K for the 5-dataset mean (4 reanalysis plus AMLS) in the satellite era, which
451 exceeds the 95% confidence level for the 5-dataset mean. The difference in temperature
452 QBO amplitude between JRA-55 and ERA5 is relatively small during the satellite era and
453 the 1970s. The temperature QBO amplitude for JRA-3Q is deviated from JRA-55 or ERA5
454 in the 1960s and earlier.

455

456 4.2 Trends of the QBO amplitude and period

457 As we saw some increasing tendency of QBO periods in the 2010s, we conduct the trend
458 analysis during the post-satellite era. Figure 8 presents the time series of QBO periods and
459 amplitudes for zonal wind at 20 hPa and temperature at 10 hPa, using JRA-3Q and other
460 datasets. Linear regression lines are plotted for the period from 1982 to 2020 to mitigate
461 edge effects in the wavelet analysis data from the post-satellite era.

462 The period of the zonal wind QBO at 20 hPa ranges from 24 to 36 months in both JRA-
463 3Q and radiosonde data. There seems decadal variation, or there are clusters of shorter
464 and longer periods. A linear regression indicates less than 1 mon de^{-1} with no confidence,
465 suggesting that this may just be an artifact of random variability. For the QBO amplitude,
466 JRA-3Q shows a flattened trend while the radiosonde exhibits a decreasing trend. The
467 temperature QBO exhibits similar behavior to the zonal wind QBO.

468 Figure 9 depicts the vertical profile of QBO amplitude trends and peak-period trends for
469 the reanalyses and observational data during the satellite era. To assess the statistical
470 significance of trends, an effective, decorrelation time for the QBO is assumed to be 14
471 months. Overall, trends of QBO periods and amplitudes have lack of confidence. There is
472 confidence in the upper stratosphere for both the QBO amplitude and period although this
473 does appear to target less important situations where the QBO amplitudes are starting to
474 drop off and the signal is ceasing to dominate SAO and AAN. In the middle-to-lower
475 stratosphere, many datasets exhibit decreasing trends of QBO amplitude without the
476 statistical significance. The QBO periods of the power peaks of zonal wind and temperature
477 exhibit consistent pattern from the lower-to-middle stratosphere, and this similarity comes
478 from the fact that the radiosonde dataset is largely constraining the reanalyses.

479 The QBO phase transition exhibits quasi-decadal variations, occasionally synchronizing
480 with the seasonal cycle (Hampson and Haynes 2004; Read and Castrejón-Pita 2012; Anstey
481 and Shepherd 2014). Figure 10 illustrates the time series of the seasonal march of zonal-
482 mean zonal wind at 20 hPa. To visualize the QBO phase transitions and their alignment with
483 the annual cycle, the x-axis represents a 2-year interval (i.e., 25 months) and the y-axis
484 displays data every two years. During the satellite era, the QBOs exhibit strikingly similar
485 characteristics in terms of periods, amplitude, phase transition between westerlies and
486 easterlies across various reanalyses, including JRA-55C. Notably, JRA-3Q shows smaller
487 easterly anomalies compared with JRA-55 and ERA5. In this figure, there are periods in

488 1970s and 1980s where the phase angle drifts at approximately a fixed rate with respect to
489 the annual cycle, whereas the 1990s and 2000s show seasonal synchronization,
490 corresponding to times with little or no drift (Anstey and Shepherd 2014). However, the
491 previous figure of the trend analysis indicated that at the 20–30 hPa levels, the peak-period
492 of the QBO exhibits an increasing trend. This apparent trend of the QBO period can be
493 primarily attributed to the stagnation of the QBO phase transition in the 2010s, potentially
494 influenced by the QBO disruption in 2016.

495

496 4.3 Latitudinal and longitudinal variations of the QBO amplitude

497 Figure 11 depicts the latitudinal distribution of the QBO amplitude in zonal wind and
498 temperature for the reanalyses and AMLS during the satellite era. Gray lines in Figs. 11b
499 and 11d represent the 95% confidence level in smoothing in time and scale against the red
500 noise background field averaged over the four reanalyses. It is noted that the smoothing
501 procedure increase the DOF, thereby enhancing confidence in regions of significant power.
502 The zonal wind QBO peaks in the mid-stratosphere with a half-width of 12° – 13° in latitude
503 (Fig. 11a, b), whereas the temperature peak occurs slightly below the wind peak with a
504 narrower half-width of approximately 10° (Figs. 11c, d). The temperature peak is linked to
505 the vertical shear of the zonal wind below the descending QBO phase. The temperature
506 anomaly extends into the subtropics, with clear subtropical lobes in the temperature
507 amplitude at 5 hPa down to 50 hPa in the Northern Hemisphere, though they are much less

508 pronounced in the Southern Hemisphere, indicative of the QBO mean meridional circulation
509 (Plumb and Bell 1982). Overall, the latitudinal structure remains consistent across the
510 reanalyses. However, the JRA-3Q QBO amplitude is reduced by 10% and 3%–4% for zonal
511 wind and temperature, respectively, compared with the other reanalyses. This amplitude
512 reduction was probably caused by stronger vertical diffusion and stronger nonorographic
513 GWD flux.

514 The longitudinal distribution of QBO amplitude at the equator is further examined in Fig.
515 12, which presents a longitude-height cross section of the zonal wind QBO amplitude and
516 its anomaly from the zonal mean. At higher altitudes, a wave-1 structure with positive and
517 negative amplitude anomalies, approximately 1 m s^{-1} in magnitude, dominates the Eastern
518 and Western Hemispheres, respectively, with a westward tilt with height in the lower-to-
519 middle stratosphere. In the lowermost stratosphere, larger amplitudes of the zonal wind
520 QBO are observed over the central Pacific with anomaly magnitude reaching up to 1 m s^{-1} ,
521 while amplitudes in the Western Hemisphere are smaller. Overall, the characteristics of
522 zonal wind QBO amplitude in the longitude-height section are consistent across the
523 reanalyses.

524 The meridional propagation of the extratropical quasi-stationary wave in the winter
525 Hemisphere leads to zonal asymmetry of the QBO amplitude in the middle stratosphere
526 (Hamilton et al. 2004). More specifically, this zonal asymmetry can be partly attributable to
527 the mode structures of quasi-stationary equatorial Rossby and Kelvin waves during strong

528 westerly and easterly phase of the QBO (Sakazaki and Hamilton 2022). In the lower
529 stratosphere the zonal asymmetries may reflect the upward extension of the tropospheric
530 Walker circulation (Hamilton et al. 2004).

531 Figure 13 illustrates the longitudinal distribution of temperature QBO amplitude and its
532 anomalies from the zonal mean at the equator. In the middle stratosphere, the temperature
533 QBO has an amplitude of 1–2 K, and a wave-1 structure with negative and positive
534 anomalies of approximately 0.1 K in the Eastern and Western Hemispheres, respectively, is
535 evident across the reanalyses. In the lower stratosphere, smaller-scale anomalies are
536 present with a local maximum over Indonesia as identified in a previous study (Tegtmeier et
537 al. 2020). However, the detailed structures differ among the reanalyses. Zonal asymmetries
538 are prominent in the temperature signal, with the QBO amplitude in the Indonesian region
539 being approximately 10%–20% larger than the zonal-mean amplitude. This result is
540 attributed to Kelvin wave variability near the equatorial tropopause, which modulates the
541 climatological cold tropopause over Indonesia. Enhanced wave amplitudes coincide with the
542 descending phase of the QBO-W (Randel and Wu, 2005).

543 The most distinct characteristics observed are the apparent disconnection of the
544 temperature QBO anomalies between the lower and middle stratosphere in JRA-55, ERA5,
545 and MERRA-2. The amplitude anomalies of JRA-3Q temperature QBO exhibit an eastward
546 tilt with height in the lower-to-middle stratosphere. Clear positive anomalies around 120°E
547 at 20–30 hPa are found in ERA5 and MERRA-2, whereas a less pronounced anomaly is

548 seen in JRA-55. The underlying reasons for these anomalies are currently unknown. One
549 possible explanation is that, although the assimilation of satellite observations does not
550 significantly impact the representation of the QBO wind evolution, inconsistency may arise
551 in the temperature field due to the data assimilation process. This involves combining
552 radiosonde winds and satellite radiance data, with the vertical weighting function associated
553 with different channels of nadir-sounding instruments potentially contributing these
554 anomalies. Another possible explanation is that ozone distribution (input or modelled) that is
555 used for radiative process in the forecast model might differ from reality. Further studies are
556 needed to explore the consistency and impacts of the radiosonde winds on the data
557 assimilation system.

558

559 **5. Discussion and Conclusion**

560 We evaluated the representation of the JRA-3Q QBO in zonal wind and temperature,
561 with a focus on its temporal consistency during both the post- and pre-satellite eras. To
562 achieve this, we compared the low-frequency variability and trends in the JRA-3Q QBO
563 during the post-satellite era with those from other reanalyses, including JRA-55, -55C, ERA5,
564 and MERRA2, as well as observational datasets. Owing to the lack of global coverage in
565 observational datasets during the pre-satellite era, the JRA-3Q QBO was also compared
566 with other reanalyses and analyzed between the post- and pre-satellite eras. A novel feature
567 of the validation methods employed is the quantification of the extent of disagreement
568 between the post- and pre-satellite eras, derived from the red noise background spectrum
569 based on the post-satellite era.

570 Here we answer several questions regarding the representation of the JRA-3Q QBO
571 raised in Introduction. 1) How well does JRA-3Q representation of the QBO align with other
572 datasets? As described in Section 3.2, the introduction of the nonorographic GWD
573 contributed to improving the representation of the QBO in reanalyses to some extent. The
574 forecast models in the latest reanalyses resolved the stratosphere to exhibit an observed-
575 QBO-like oscillation in zonal-mean zonal wind. Overall, almost all reanalyses showed good
576 agreement with each other and with the sonde data, and there is a marked convergence
577 over latest 15 years (from the late 2010s to onward).

578 2) To what extent can we quantify differences in the representation of the QBO among

579 reanalyses and observations? The JRA-3Q QBOs in zonal wind and temperature during the
580 satellite era were slightly reduced compared with other reanalyses such as JRA-55, ERA5,
581 and MERRA-2. Specifically, the QBO amplitudes at 20–30 hPa in JRA-3Q were reduced by
582 8% and 4%, respectively, compared with the other reanalyses. The QBO periods of the
583 power peaks were coincident across the reanalyses in the lower-to-middle stratosphere
584 owing to the radiosonde dataset largely constraining the reanalyses. QBO amplitudes seem
585 have decreasing trends in the middle-to-lower stratosphere and the QBOs in the 20–30 hPa
586 layers exhibit longer periods although most trends of QBO periods and amplitudes have lack
587 of confidence.

588 3) Is it appropriate to use reanalysis data from the pre-satellite era? We quantified the
589 disagreement between the post- and pre-satellite eras using the red noise background
590 spectrum based on the post-satellite era data. The QBO periods of the power peaks showed
591 an agreement with each other in the lower-to-middle stratosphere. However, the JRA-3Q
592 QBO from the early 1960s and before is substantially degraded, falling below the 95%
593 confidence level. In contrast, there was an improvement in the representation of the JRA-
594 3Q ANN in the equatorial stratosphere, whereas the JRA-55 ANN in the pre-satellite era
595 completely disappeared due to unrealistically strong damping in the model's upper layers.

596 4) Are there specific aspects of the JRA-3Q QBO that should be considered when using
597 it? Overall, the latitudinal structure is consistent among the reanalyses, with the exception
598 of the amplitude in JRA-3Q. The zonal asymmetry of the zonal wind QBO amplitude is

599 dominated by a wave-1 structure with a magnitude of about 1 m s^{-1} in the middle-to-upper
600 stratosphere. Larger amplitudes of the zonal wind QBO are observed over the central Pacific,
601 while smaller amplitudes are present in the Western Hemisphere, with magnitudes up to 1
602 m s^{-1} , in agreement with previous studies. In the lowermost stratosphere, smaller-scale
603 anomalies of the temperature QBO amplitude with a local maximum over Indonesia are
604 evident, as identified in previous studies. However, the detailed structures of these
605 anomalies differ among the reanalyses. One of the most distinct characteristics of these
606 zonal asymmetries is the disconnection of the temperature QBO anomalies between the
607 lower and middle stratosphere in JRA-55, ERA5 and MERRA-2. Additionally, the amplitude
608 anomalies of the JRA-3Q temperature QBO exhibit an eastward tilt with height in the lower-
609 to-middle stratosphere. The underlying reasons for these anomalies are currently unknown.
610 Possible explanations are that data assimilation between radiosonde winds and satellite
611 radiance may introduce inconsistencies in the temperature field or that input or modelled
612 ozone distribution might be different from reality.

613 In conclusion, the forecast models in the latest reanalyses presented in this paper still
614 exhibit numerous biases, indicating that further improvements are needed to enhance their
615 representation for more accurate diagnostics. Critical deficiencies in QBO-resolving models
616 include inaccuracies in the mean QBO period and amplitude, the latitudinal width, especially
617 latitudinal and vertical extents in the lower stratosphere, the vertical width, and other related
618 factors (Bushell et al. 2020; Schenzinger et al. 2017). Improving these factors, especially in

619 a pre-satellite era, is particularly important for capturing tropical variability in the stratosphere
620 and QBO teleconnections within both extratropical circulation and the tropical troposphere.

621 The double challenging issues raised in Section 3.2 would have a broader applicability
622 than simply development of reanalysis systems, and understanding their limitations, due to
623 the recent explosion of machine learning activity for meteorology and its reliance on
624 reanalysis data for training and testing. There are clear implications for anyone seeking to
625 use reanalyses in this context for QBO prediction if the data covers an era when reanalyses
626 show divergent behavior. There are also implications for those attempting to avoid
627 dependence on reanalysis products by ingesting observations directly if this does not
628 guarantee realistic QBO properties.

629 Finally, state-of-the-art current data assimilation systems are characterized by
630 background error covariances with shorter horizontal correlation lengths compared to their
631 predecessor (Kosaka et al. 2024). Artificial changes can arise due to variations in the quality
632 and quantity of input observational data, especially before and after satellite data, after the
633 introduction of the AMSU satellite observations around 1998, and the absence of tropical
634 radiosonde data. Therefore, next-generation reanalysis projects will adopt or implement
635 appropriate background error-correlation lengths over the course of time, especially during
636 significant discontinuities in the input observational data.

637

638

639 **Appendix**

640 Following Torrence and Compo (1998), this Appendix describes the statistical significance
641 tests for wavelet spectrum.

642

643 a. Wavelet transform

644 Consider a time series of signal, x_n , with equal time spacing δt and the time index $n = 0$
645 ... $N - 1$. The wavelet transform, $W_n(s)$, is defined as the convolution of x_n with the wavelet
646 scale s . By the convolution theorem, the wavelet transform is expected using the wavelet
647 function ψ :

$$648 \quad W_n(s) = \sum_{k=0}^{N-1} x_k \psi^*(s\omega_k) e^{i\omega_k n \delta t}, \quad (\text{a1})$$

649 where $k = 0 \dots N - 1$ is the frequency index, ω_k is the angular frequency, and (*) denotes
650 the complex conjugate.

651 The total energy is conserved in the wavelet transform, and the equivalent *Parseval's*
652 *theorem* for wavelet analysis is given by:

$$653 \quad \sigma^2 = \frac{\delta j \delta t}{C_\delta N} \sum_{n=0}^{N-1} \sum_{j=0}^J \frac{|W_n(s_j)|^2}{s_j}, \quad (\text{a2})$$

654 where σ denotes the variance, j represents the wavelet scale index, and $\delta j = 0.125$, C_δ
655 = 0.776.

656

657 b. Smoothing in time and scale

658 The time-averaged wavelet spectrum over a certain period is defined as

$$659 \quad W_n^2(s) = \frac{1}{n_a} \sum_{n_1}^{n_2} |W_n(s)|^2, \quad (\text{a3})$$

660 where $n_a = n_2 - n_1 + 1$ denotes the number of points averaged over. The time-averaged
 661 confidence level is best described by the distribution $P_k \chi_\nu^2 / \nu$, where P_k is the original
 662 assumed background spectrum, and χ_ν^2 follows a chi-square distribution with ν DOF:

$$663 \quad \nu = 2\sqrt{1 + f_T^2}, \quad f_T = \frac{n_a \delta t}{\gamma s}, \quad (\text{a4})$$

664 where n_a represents number of points averaged over, δt denotes the time step, and
 665 $\gamma = 2.32$.

666 The scale-averaged wavelet power can be defined as the weighted sum of the
 667 wavelet power spectrum over scales s_1 to s_2 :

$$668 \quad \overline{W_n^2} = \frac{\delta j \delta t}{C_\delta} \sum_{j_1}^{j_2} \frac{|W_n(s_j)|^2}{s_j}. \quad (\text{a5})$$

669 where $\delta j = 0.125$, $\delta j_0 = 0.6$. The DOF ν for the scale-averaged wavelet power spectrum
 670 can be modeled as

$$671 \quad \nu = \frac{2n_b S_{avg}}{S_{mid}} \sqrt{1 + f_S^2}, \quad f_S = \frac{n_a \delta j}{\delta j_0}, \quad (\text{a6})$$

672 where n_b represents the number of scales averaged over, $S_{mid} = s_2 2^{(j_1 + j_2) d_j / 2}$, and S_{avg}
 673 is defined as

$$674 \quad S_{avg} = \left(\sum_{j=j_1}^{j_2} \frac{1}{s_j} \right)^{-1}. \quad (\text{a7})$$

675 Similarly, the DOF ν for the time-and-scale-averaged wavelet power spectrum can be
 676 modeled as

$$677 \quad \nu = \frac{2n_b S_{avg}}{S_{mid}} \sqrt{1 + f_S^2} \sqrt{1 + f_T^2} \sqrt[4]{1 + f_S f_T}. \quad (\text{a8})$$

678

679

680 Data Availability Statement

681 The JRA-3Q and JRA-55 reanalysis data are accessible through collaborative organizations
682 listed in the JRA website (<https://jra.kishou.go.jp>). The ERA5 reanalysis data can be
683 obtained from the ECMWF website ([https://www.ecmwf.int/en/forecasts/datasets/browse-
684 reanalysis-datasets](https://www.ecmwf.int/en/forecasts/datasets/browse-reanalysis-datasets)). Similarly, the MERRA-2 reanalysis data can be obtained from the
685 NASA website (<https://disc.gsfc.nasa.gov/datasets/>).

686 Monthly temperature and geopotential height data from the MLS instrument can be obtained
687 from the NASA website (https://acdisc.gesdisc.eosdis.nasa.gov/data/Aura_MLS_Level3/).

688

689 Supplement

690 Supplement 1 represents the power spectra of zonal-mean temperature (Figure S1).

691 Supplement 2 displays the time series of profile of wavelet power amplitude of temperature
692 (Figure S2).

693

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921

922 List of Figures

923 Fig. 1. Time series of monthly zonal-mean zonal wind averaged over 5°S and 5°N for (a)
924 JRA-3Q, (b) JRA-55, (c) ERA5, (d) MERRA-2, (e) AURA/MLS (AMLS), and (e) combined
925 radiosonde observations at the equator. AMLS zonal wind is estimated from the
926 geostrophic balance using the AMLS monthly 3D temperature field. Radiosonde data are
927 derived from three stations: Canton Island (2.8°S, 171.7°W) from 1953 to 1967,
928 Gan/Maldives (0.7°S, 73.15°E) from 1967 to 1975, and Singapore (1.4°N, 103.9°E) from
929 1953 to 2023.

930

931 Fig. 2. Power spectra of zonal-mean zonal wind averaged over 10°S and 10°N from 100
932 hPa to 1 hPa during a post-satellite era 2003–2022 for (a) JRA-3Q, (b) MERRA-2, and (c)
933 ERA5. Power spectra during pre-satellite eras for (d) 1948–1967 JRA-3Q, (e) 1958–1977
934 JRA-55 and (f) 1948–1967 ERA5. Values are displayed on a logarithmic scale of base 10
935 and are expressed in units of $\text{m}^2 \text{s}^{-2}$. The contour interval is 0.4.

936

937 Fig. 3. (a) Wavelet power spectrum of zonal-mean zonal wind at the equator (5°S–5°N) at
938 20 hPa in JRA-3Q. The thin gray line represents the mean red noise spectrum (theoretical
939 background noise) with an AR(1) of 0.94. The upper thick gray line represents the 95%
940 confidence spectrum, assuming the square of a normally distributed variable being chi-
941 square distributed with one DOF for each real and imaginary part of the complex wavelet

942 transform function. A green line indicates the spectrum of zonal wind power taken at time
943 January 2010, normalized by variance. (b) The 21-year averaged power spectrum along
944 with the 95% confidence level, and the DOF is increased by averaging in time and scale.

945

946 Fig. 4. Time series of the wavelet power spectrum of zonal-mean zonal wind at 20 hPa at
947 the equator (5°S – 5°N) over the period ranging from 9 to 60 months. The COI is
948 represented by cross hatching.

949

950 Fig. 5. Time series profile of wavelet power amplitude of zonal wind (m s^{-1}) for (a) JRA-3Q,
951 (b) JRA-55, (c) ERA5, (d) MERRA-2, (e) AMLS, and (f) the sonde data. The QBO is
952 defined in wavelet power spectrum from 20 to 40 months, and the power amplitude is
953 considered to be square root of twice the power. The dot indicates the confidence below
954 the 95% level, based on the background red noise taken from the post-satellite era from
955 1980 to 2022.

956

957 Fig. 6. Wavelet power amplitude (blue) and direct-method amplitude (red) of zonal-mean
958 zonal wind QBO (m s^{-1}) at 20 hPa in JRA-3Q. A black solid line represents the absolute
959 of band-pass filtered data averaged between 5°S and 5°N , with star marks indicating the
960 minimum of the square of the band-passed data. A horizontal gray line denotes the 95%
961 confidence level of the wavelet power over the range of 20 to 40 months.

962

963 Fig. 7. Time series of wavelet power amplitude for (a) zonal wind at 20 hPa and (b)
964 temperature at 30 hPa for JRA-3Q (red), JRA-55 (blue), ERA5 (green), MERRA-2 (yellow),
965 AMLS (orange), and sonde observations (purple). The gray horizontal line represents the
966 95% confidence level of the red noise averaged over the four reanalysis datasets,
967 evaluated from data spanning 1980–2022. The solid part of the horizontal line covers the
968 period from 1982 to 2020, while the dashed part covers the period from 1940 to 1981 and
969 after 2020.

970

971 Fig. 8. (a) Time series of the average period (months) of the three largest components in the
972 local wavelet power of the zonal-mean zonal wind at 20 hPa for (a) JRA-3Q (black), along
973 with a linear regression (red) during the period from 1982 to 2020. (b) Same as (a) but for
974 the radiosonde observations (gray), with a linear regression (purple). (c) QBO amplitude
975 of zonal wind (m s^{-1}) at 20 hPa by the wavelet method for JRA-3Q and radiosonde
976 observations. (d) Same as (a) but for zonal-mean temperature at 10 hPa. (e) Same as (b)
977 but for ERA5 (gray) with a linear regression (green). (f) Same as (c) but for QBO amplitude
978 of temperature (K) at 10 hPa for JRA-3Q and ERA5.

979

980 Fig. 9. Vertical profile of trends in (a) QBO amplitude and (b) power-peak period of zonal
981 wind at the equator during the satellite era from 1982 to 2020. Data are presented for

982 JRA-3Q, JRA-55, ERA5, MERRA-2, and the radiosonde observations. Circles stand for
983 the statistical significance at the 95% level. The effective decorrelation time for the QBO
984 is assumed to be 14 months. (c) and (d), same as (a) and (b) but for temperature.

985

986 Fig. 10. Time-series of the seasonal march of zonal-mean zonal wind at 20 hPa. The x-axis
987 spans 25 months to visualize the seasonal march of the QBO, while the y-axis represents
988 data every two years. (a) JRA-3Q, (b) JRA-55, (c) ERA5, (d) AMLS, and (e) JRA-55C.

989

990 Fig. 11. (a) Latitude-height cross section of zonal wind QBO amplitude (m s^{-1}) in a satellite-
991 era period from 1982 to 2020 for JRA-3Q. The dot stands for the confidence level below
992 95%. (b) Latitudinal profiles of the zonal wind QBO amplitude at 20 hPa during the same
993 period for JRA-3Q (red), JRA-55 (blue), ERA5 (green), MERRA-2 (yellow), and AMLS
994 (orange), along with the mean 95% confidence level derived from the mean of four
995 reanalyses (gray). The period covered by MLS is from 2007 to 2020 to avoid data edges.
996 (c, d) Same as (a, b) but for zonal mean temperature QBO amplitude (K).

997

998 Fig. 12. Longitude-height cross section of QBO amplitude of zonal wind (m s^{-1}) at the
999 equator during the satellite era from 1982 to 2022 for (a) JRA-3Q, (b) JRA-55, (c) ERA5,
1000 and (d) MERRA-2. Shadings indicate anomalies from the zonal mean.

1001

1002 Fig. 13. Same as Fig. 12, but for QBO amplitude of temperature (K).

1003

1004

1005 Supplement figure captions

1006 Fig. S1. Power spectra of zonal-mean temperature averaged over 10°S and 10°N from 100

1007 hPa to 1 hPa during a post-satellite era 2003–2022 for (a) JRA-3Q, (b) MERRA-2, and (c)

1008 ERA5. Power spectra during pre-satellite eras for (d) 1948–1967 JRA-3Q, (e) 1958–

1009 1977 JRA-55, and (f) 1948–1967 ERA5. Values are shown on a logarithmic scale of base

1010 10, and are expressed in units of K^2 . The contour interval is 0.4.

1011

1012 Fig. S2. Time series of wavelet power amplitude profile of temperature (K) for (a) JRA-3Q,

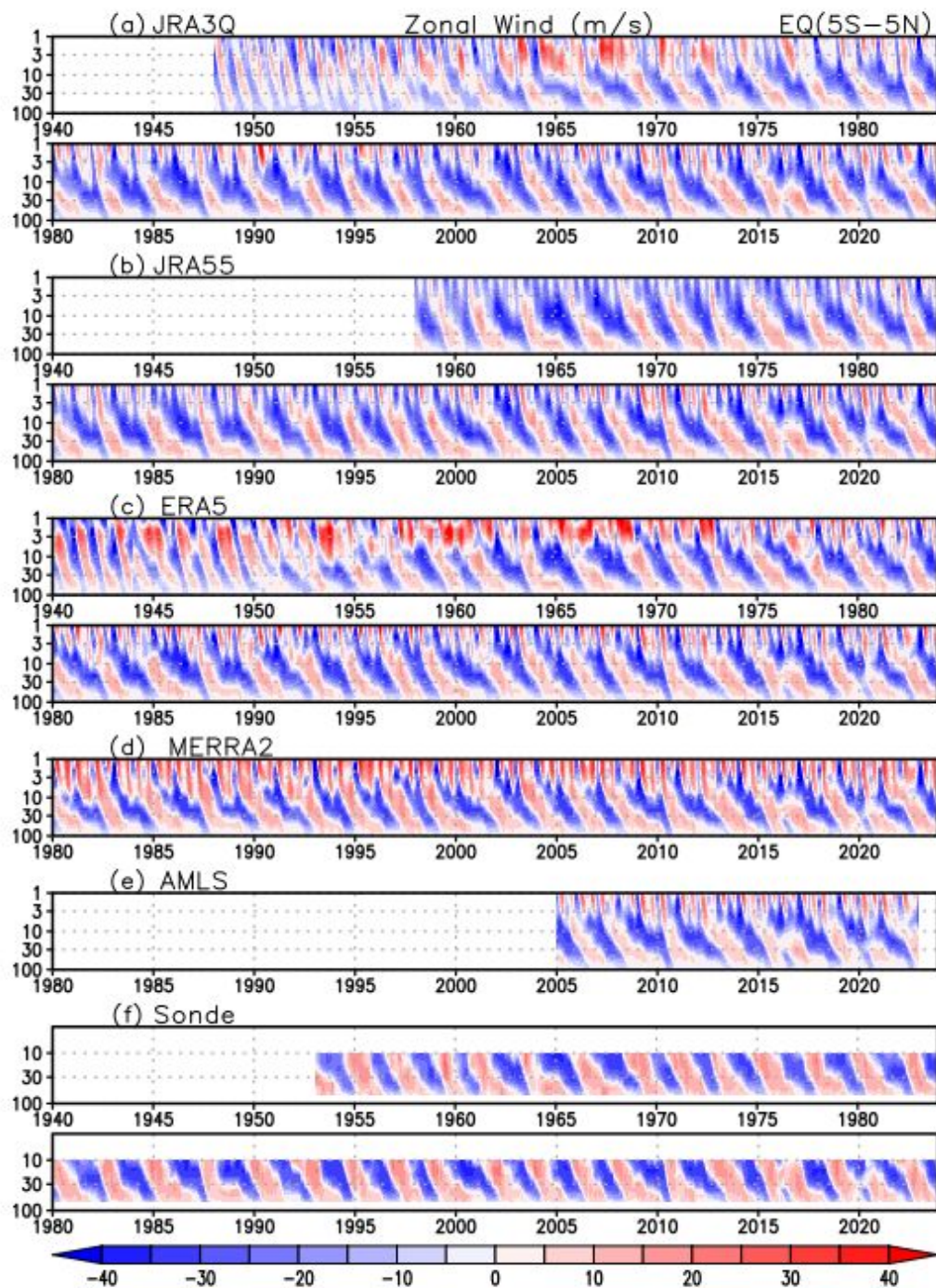
1013 (b) JRA-55, (c) ERA5, (d) MERRA-2, and (e) AMLS. The QBO is defined in the wavelet

1014 power spectrum from 20 to 40 months, with the power amplitude assumed to be square

1015 root of twice the power. The dot indicates the confidence below the 95% level, based on

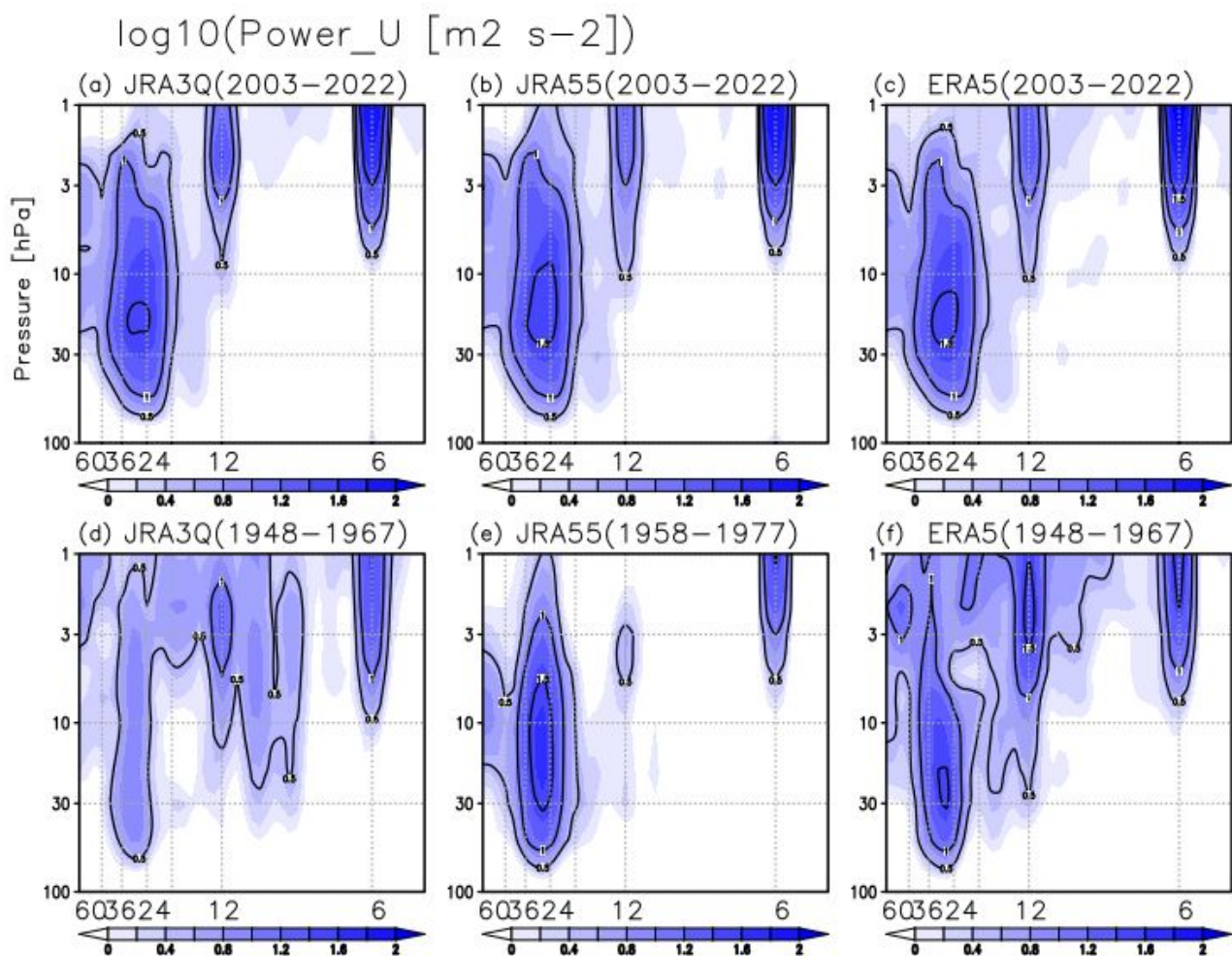
1016 the background red noise taken from the post-satellite era from 1980 to 2022.

1017



1018 Fig. 1. Time series of monthly zonal-mean zonal wind averaged over 5°S and 5°N for (a)
 1019 JRA-3Q, (b) JRA-55, (c) ERA5, (d) MERRA-2, (e) AURA/MLS (AMLS), and (e) combined
 1020 radiosonde observations at the equator. AMLS zonal wind is estimated from the
 1021 geostrophic balance using the AMLS monthly 3D temperature field. Radiosonde data are
 1022 from three stations: Canton Island (2.8°S, 171.7°W) from 1953 to 1967, Gan/Maldives
 1023 (0.7°S, 73.15°E) from 1967 to 1975, and Singapore (1.4°N, 103.9°E) from 1953 to 2023.

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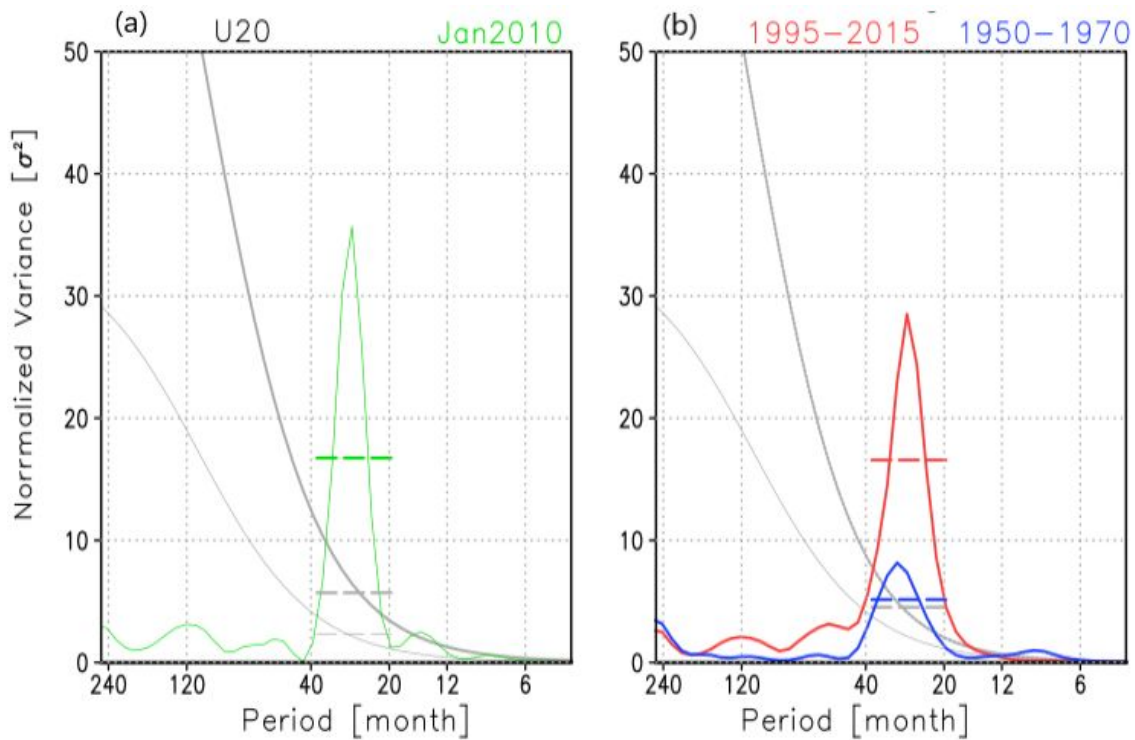


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1026

1027 Fig. 2. Power spectra of zonal-mean zonal wind averaged over 10°S and 10°N from 100
 1028 hPa to 1 hPa during a post-satellite era 2003–2022 for (a) JRA-3Q, (b) MERRA-2, and (c)
 1029 ERA5. Power spectra during pre-satellite eras for (d) 1948–1967 JRA-3Q, (e) 1958–1977
 1030 JRA-55 and (f) 1948–1967 ERA5. Values are expressed in a logarithmic scale of base 10
 1031 in units of $\text{m}^2 \text{ s}^{-2}$. The contour interval is 0.4.

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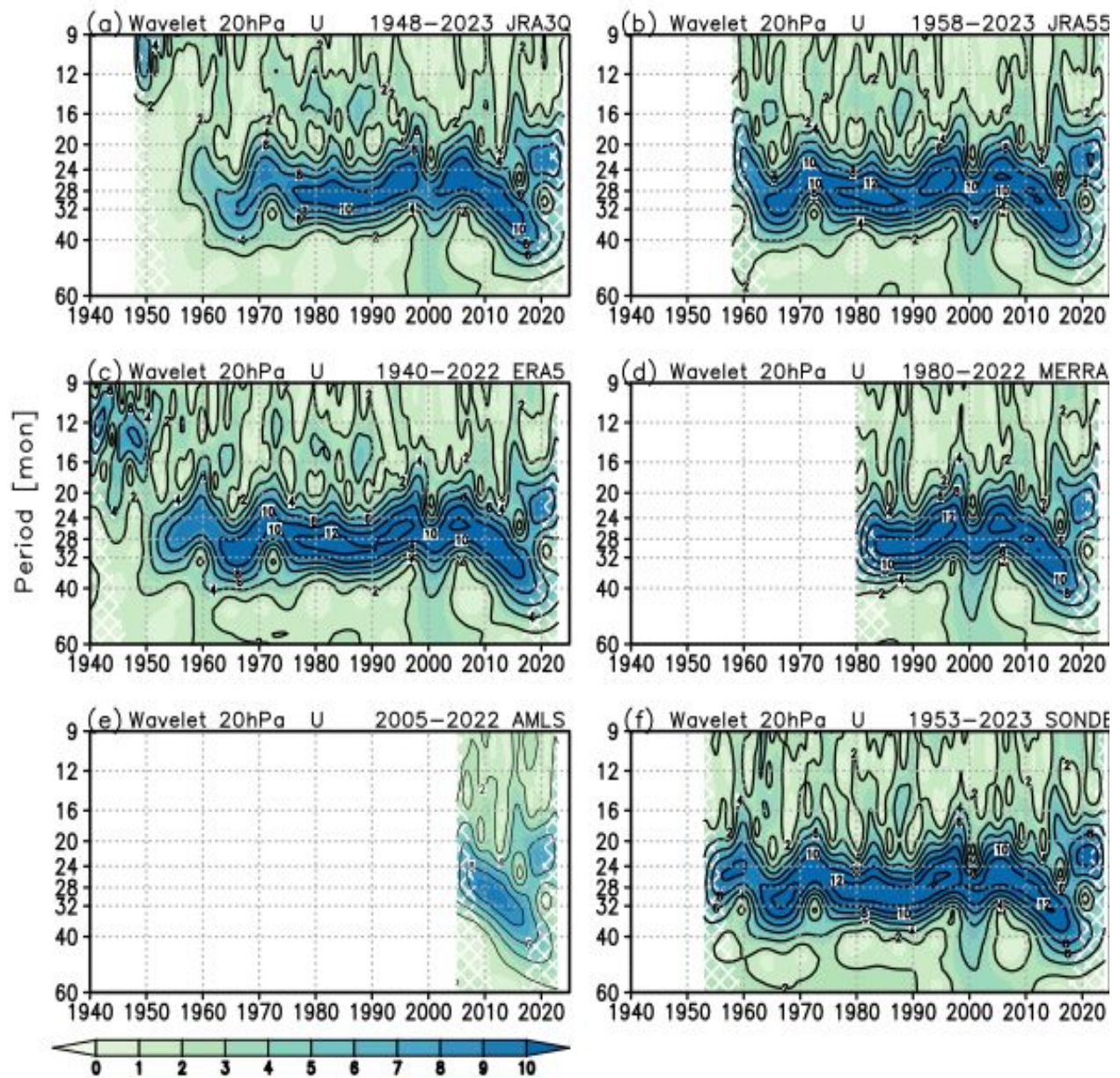


1033

1034 Fig. 3. (a) Wavelet power spectrum of zonal mean zonal wind at the equator (5°S – 5°N) at
 1035 20 hPa in JRA-3Q. The thin gray line represents the mean red noise spectrum (theoretical
 1036 background noise) with an AR(1) of 0.94. The upper thick gray line represents the 95%
 1037 confidence spectrum assuming the square of a normally distributed variable being chi-
 1038 square distributed with one DOF for each real and imaginary part of the complex wavelet
 1039 transform function. A green line indicates a spectrum of zonal wind power taken at time
 1040 January 2010, normalized by variance. (b) The 21-year averaged power spectrum along
 1041 with the 95% confidence level, and the DOF is increased by averaging in time and scale.

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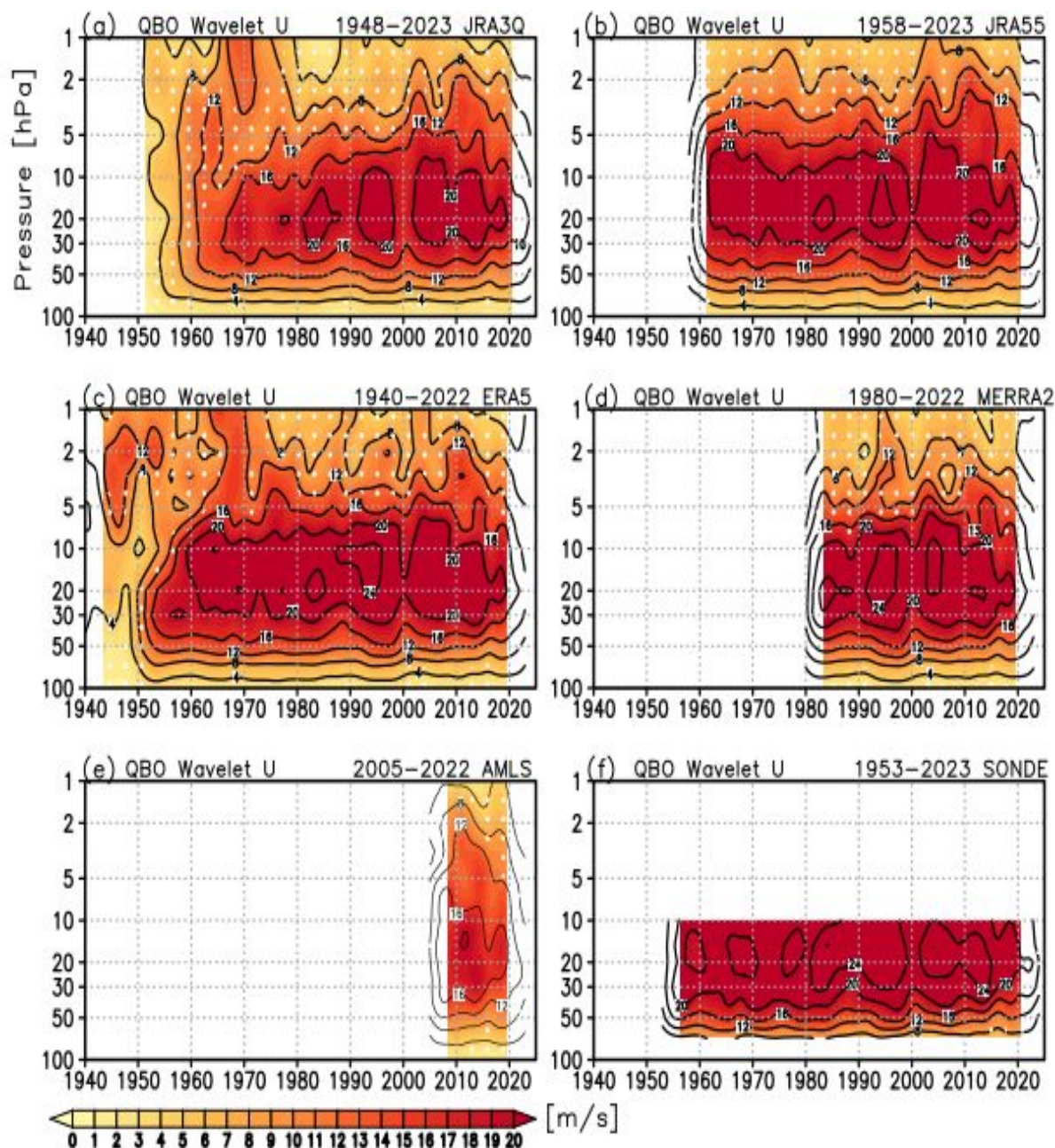
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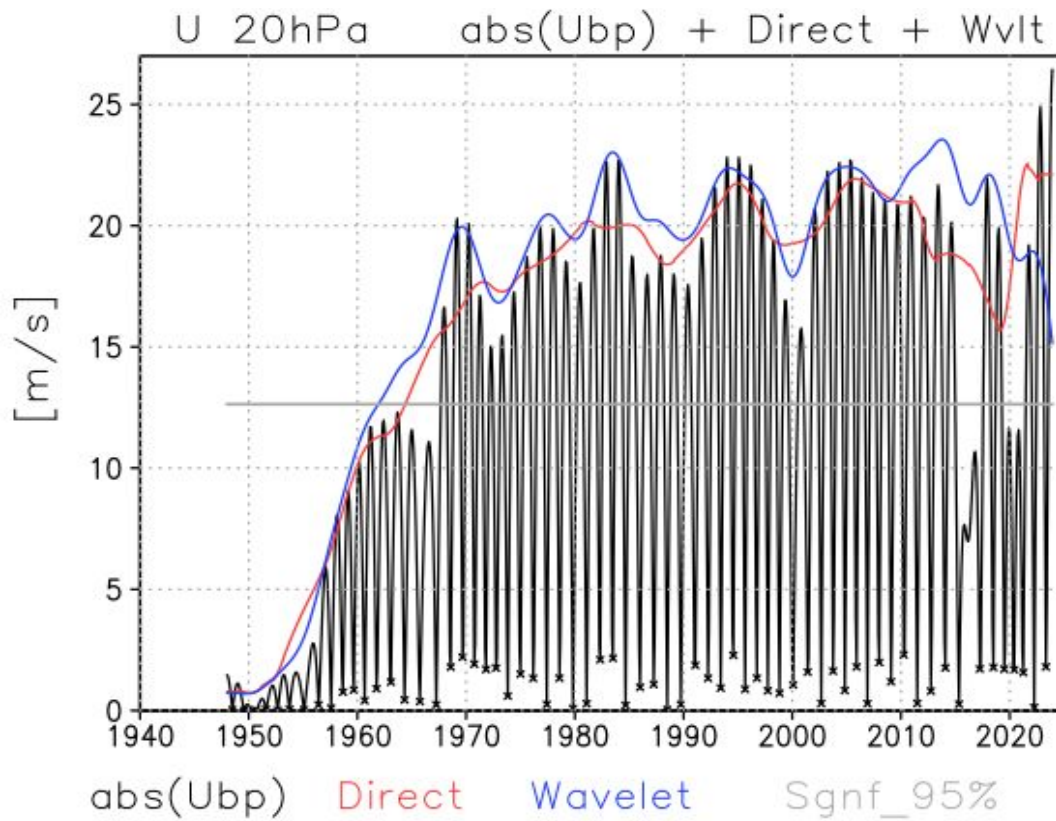
1044

1045 Fig. 4. Time series of the wavelet power spectrum of zonal-mean zonal wind at 20 hPa at
 1046 the equator (5°S – 5°N) over the period ranging from 9 to 60 months. The COI is
 1047 represented by cross hatching.

1048



1049 Fig. 5. Time series of wavelet power amplitude profile of zonal wind (m s^{-1}) for (a) JRA-3Q,
 1050 (b) JRA-55, (c) ERA5, (d) MERRA-2, (e) AMLS, and (f) the sonde data. The QBO is
 1051 defined in wavelet power spectrum from 20 to 40 months, with the power amplitude
 1052 assumed to be square root of twice the power. The dot indicates the confidence below
 1053 the 95% level, based on the background red noise taken from the post-satellite era from
 1054 1980 to 2022.

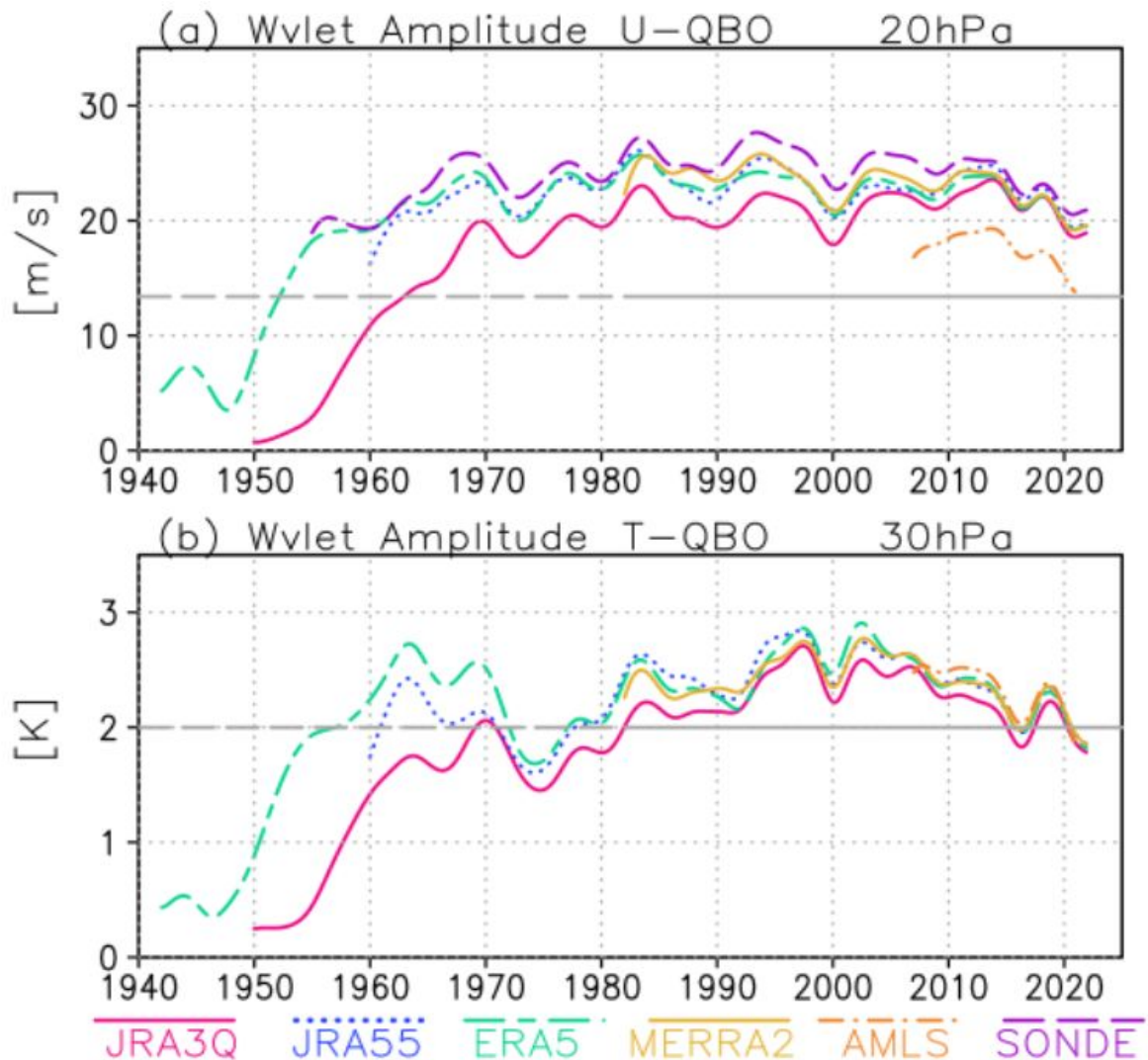


1055

1056 Fig. 6. Wavelet power amplitude (blue) and direct-method amplitude (red) of zonal-mean
 1057 zonal wind QBO (m s^{-1}) at 20 hPa in JRA-3Q. A black solid line represents the absolute
 1058 of band pass filtered data averaged between 5°S and 5°N , with star marks indicating the
 1059 minimum of the square of the band-passed data. A horizontal gray line denotes the 95%
 1060 confidence level of the wavelet power over the range of 20 to 40 months.

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1064 Fig. 7. Time series of wavelet power amplitude for (a) zonal wind at 20 hPa and (b)

1065 temperature at 30 hPa for JRA-3Q (solid magenta), JRA-55 (dotted blue), ERA5 (long

1066 short dash aqua), MERRA-2 (solid yellow), AMLS (dot dash orange), and sonde

1067 observations (long dash purple). The gray horizontal line represents the 95% confidence

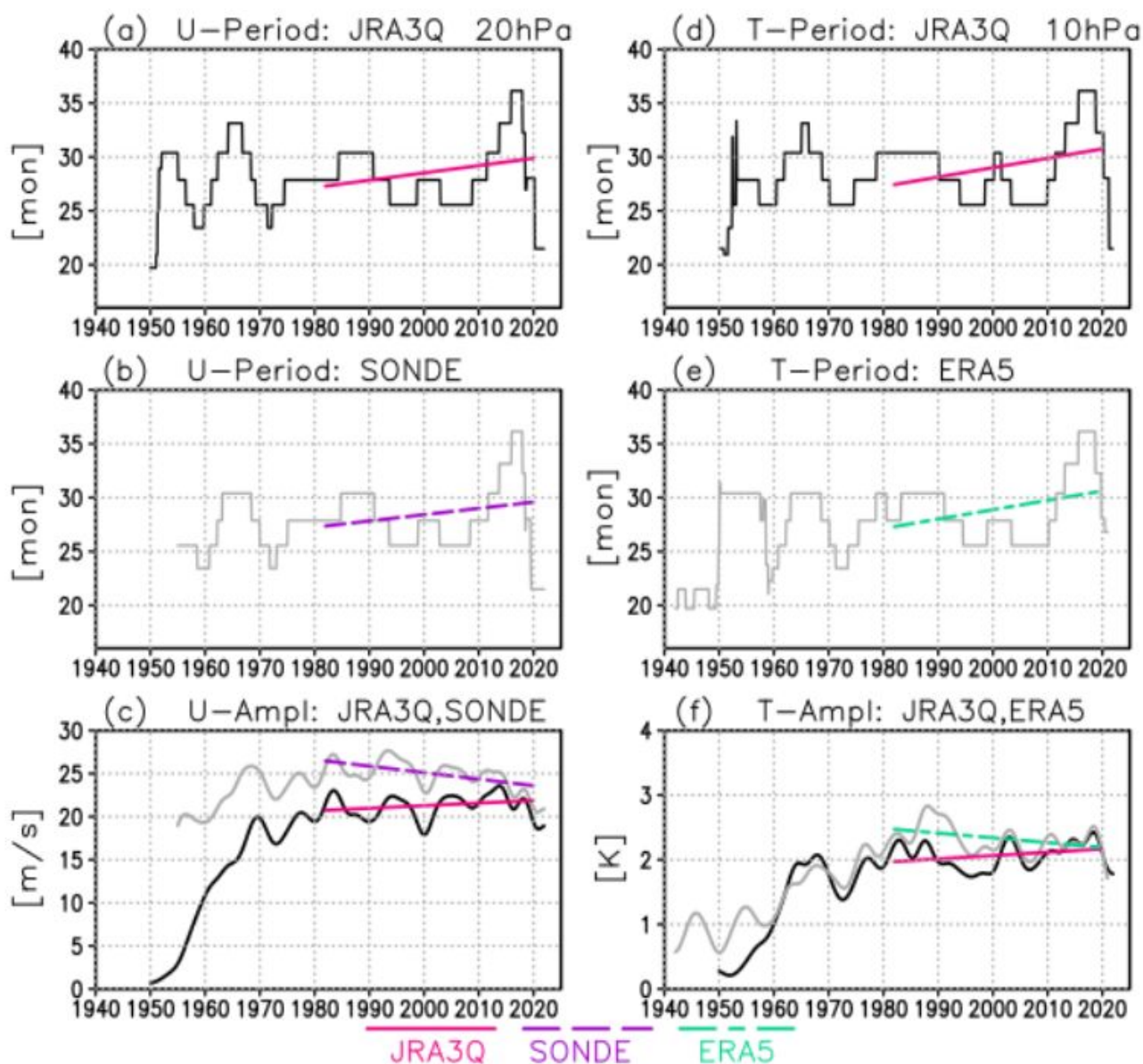
1068 level of the red noise averaged over the four reanalysis datasets, evaluated from data

1069 spanning 1980–2022. The solid part of the horizontal line covers the period from 1982 to

1070 2020, while the dashed part covers the period from 1940 to 1981 and after 2020.

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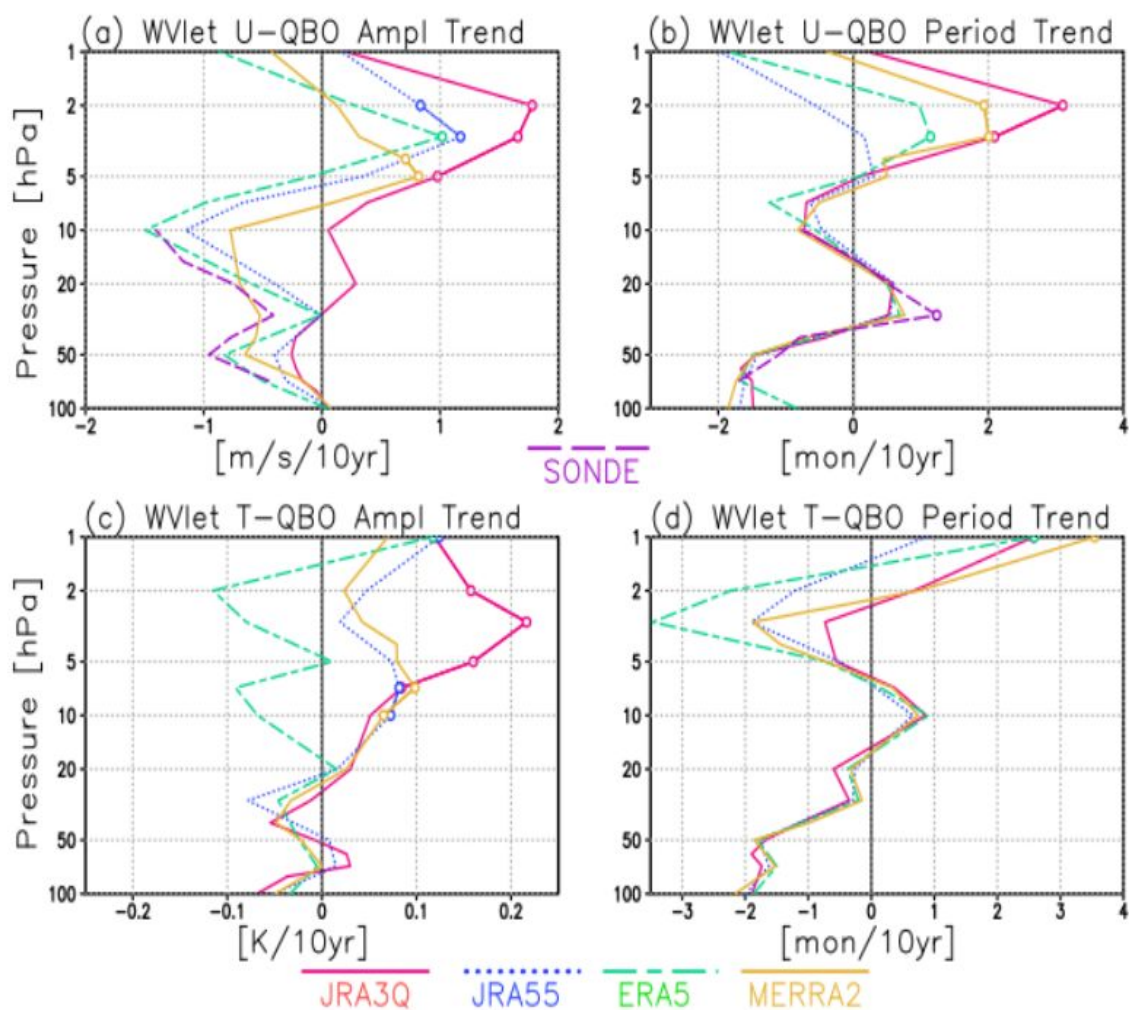


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1074 Fig. 8. (a) Time series of the average period (months) of the three largest components in the
 1075 local wavelet power of the zonal-mean zonal wind at 20 hPa for (a) JRA-3Q (black), along
 1076 with a linear regression (magenta) during the period from 1982 to 2020. (b) Same as (a)
 1077 but for radiosonde observations (gray) with a linear regression (purple). (c) QBO
 1078 amplitude of zonal wind (m s^{-1}) at 20 hPa by the wavelet method for JRA-3Q and
 1079 radiosonde observations. (d) Same as (a) but for zonal-mean temperature at 10 hPa. (e)
 1080 Same as (b) but for ERA5 (gray) with a linear regression (aqua). (f) Same as (c) but for
 1081 QBO amplitude of temperature (K) at 10 hPa for JRA-3Q and ERA5.

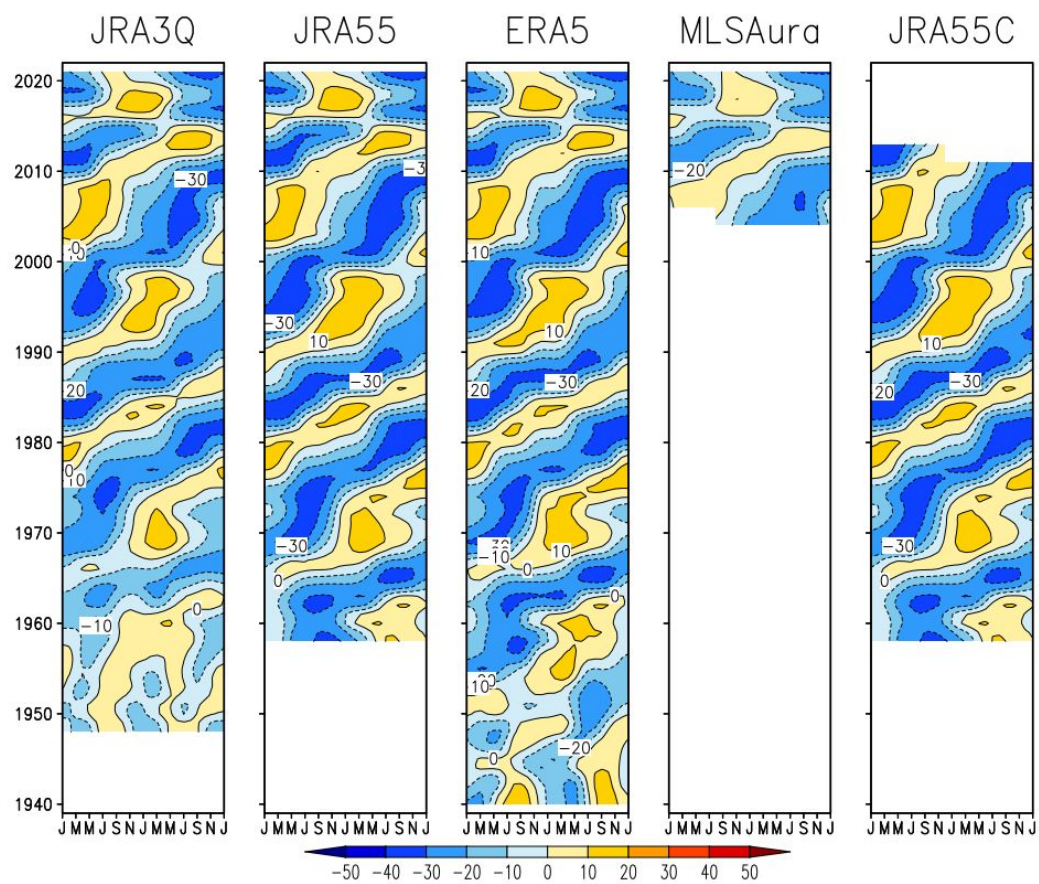
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1085 Fig. 9. Vertical profile of trends in (a) QBO amplitude and (b) power-peak period of zonal
 1086 wind at the equator during the satellite era from 1982 to 2020 for JRA-3Q, JRA-55, ERA5,
 1087 MERRA-2, and radiosonde observations. Circles stands for the statistical significance at
 1088 the 95% level. The effective decorrelation time for the QBO is assumed to be 14 months.
 1089 (c) and (d), same as (a) and (b) but for temperature.

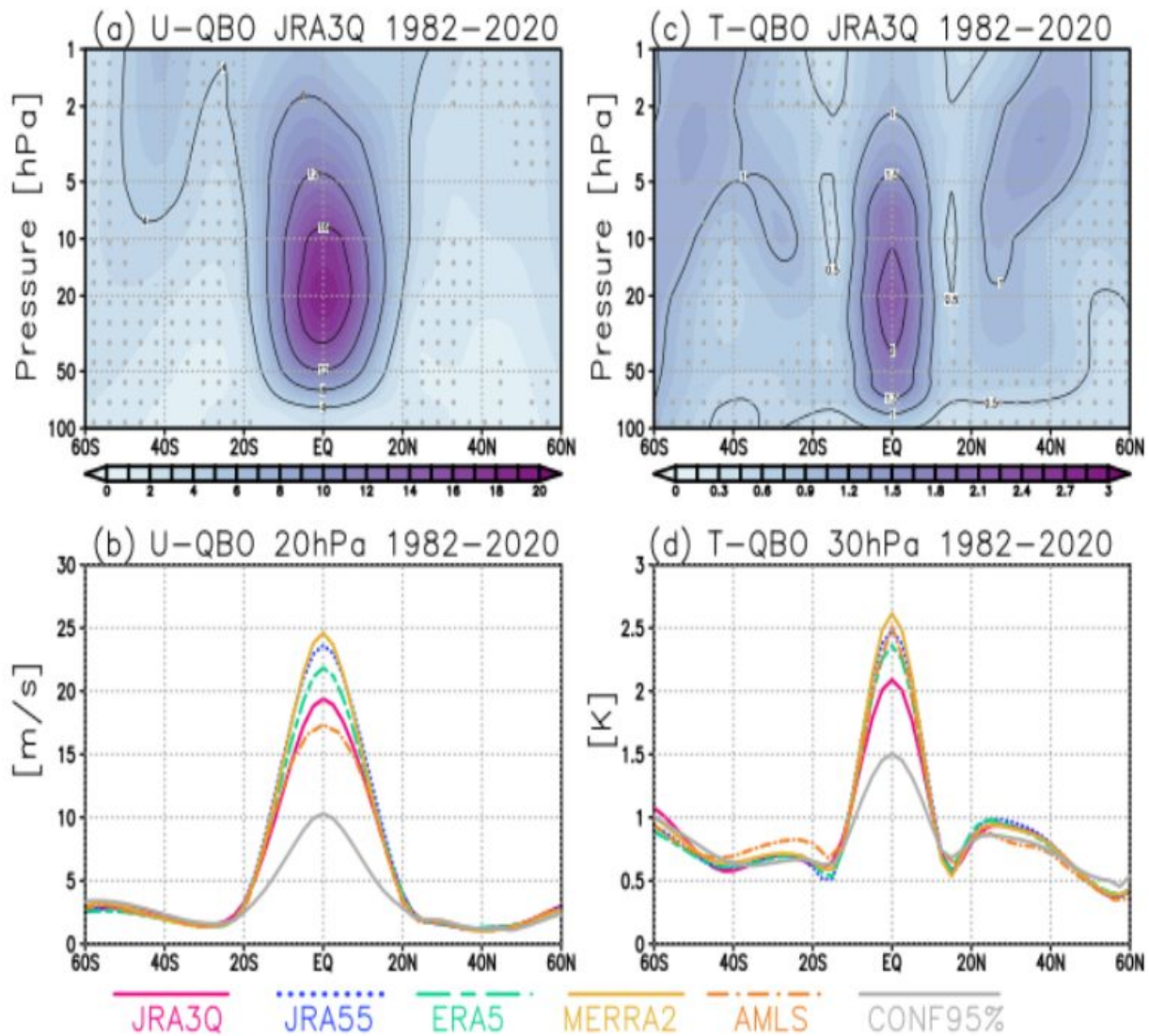


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1091 Fig. 10. Time-series of the seasonal march of zonal-mean zonal wind at 20 hPa. The x-axis
 1092 spans 25 months to visualize the seasonal march of the QBO, while the y-axis represent
 1093 data every two years. (a) JRA-3Q, (b) JRA-55, (c) ERA5, (d) AMLS, and (e) JRA-55C.

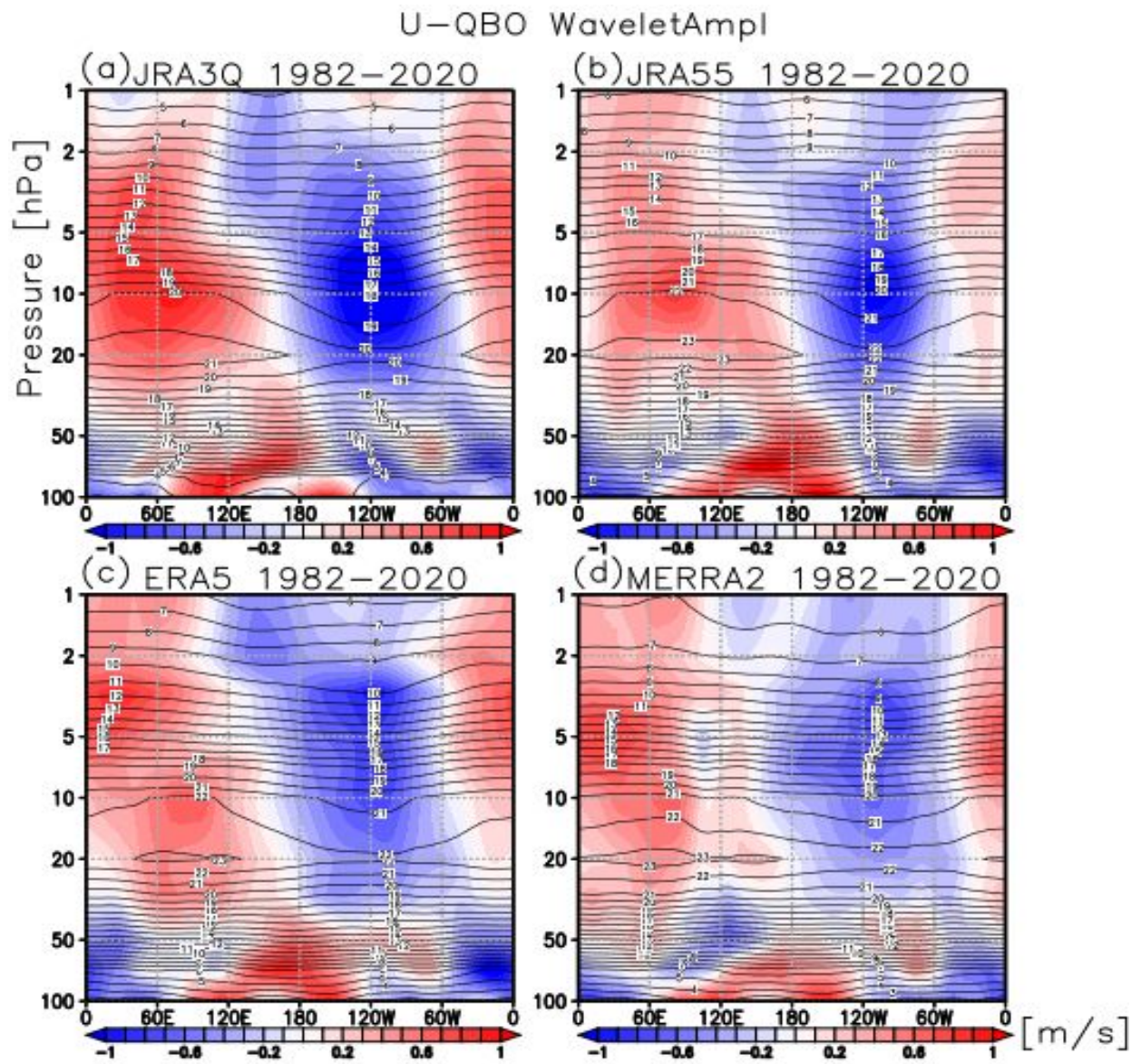
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1097 Fig. 11. (a) Latitude-height cross section of zonal wind QBO amplitude (m s^{-1}) in a satellite-
 1098 era period from 1982 to 2020 for JRA-3Q. The dot stands for the confidence level below
 1099 95%. (b) Latitudinal profiles of the zonal wind QBO amplitude at 20 hPa during the same
 1100 period for JRA-3Q (solid magenta), JRA-55 (dotted blue), ERA5 (long short dash aqua),
 1101 MERRA-2 (solid yellow), and AMLS (dot dash orange), along with the 95% confidence
 1102 level derived from the mean of four reanalyses (gray). The period covered by MLS is from
 1103 2007 to 2020 to avoid data edges. (c, d) Same as (a, b) but for zonal mean temperature
 1104 QBO amplitude (K).

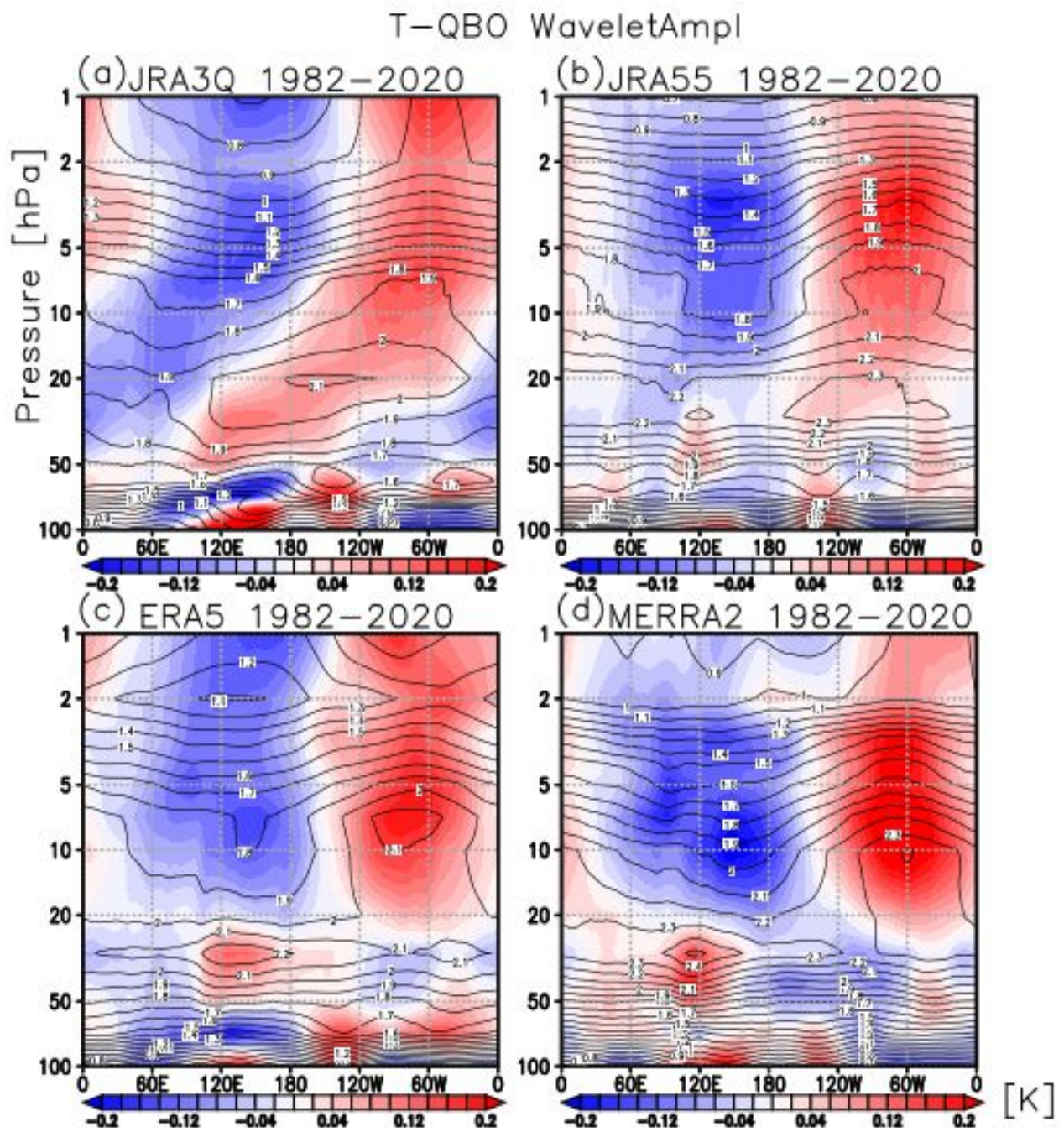


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1106 Fig. 12. Longitude-height cross section of QBO amplitude of zonal wind (m s^{-1}) at the
 1107 equator during the satellite era from 1982 to 2022 for (a) JRA-3Q, (b) JRA-55, (c) ERA5,
 1108 and (d) MERRA-2. Shadings indicate anomalies from the zonal mean.

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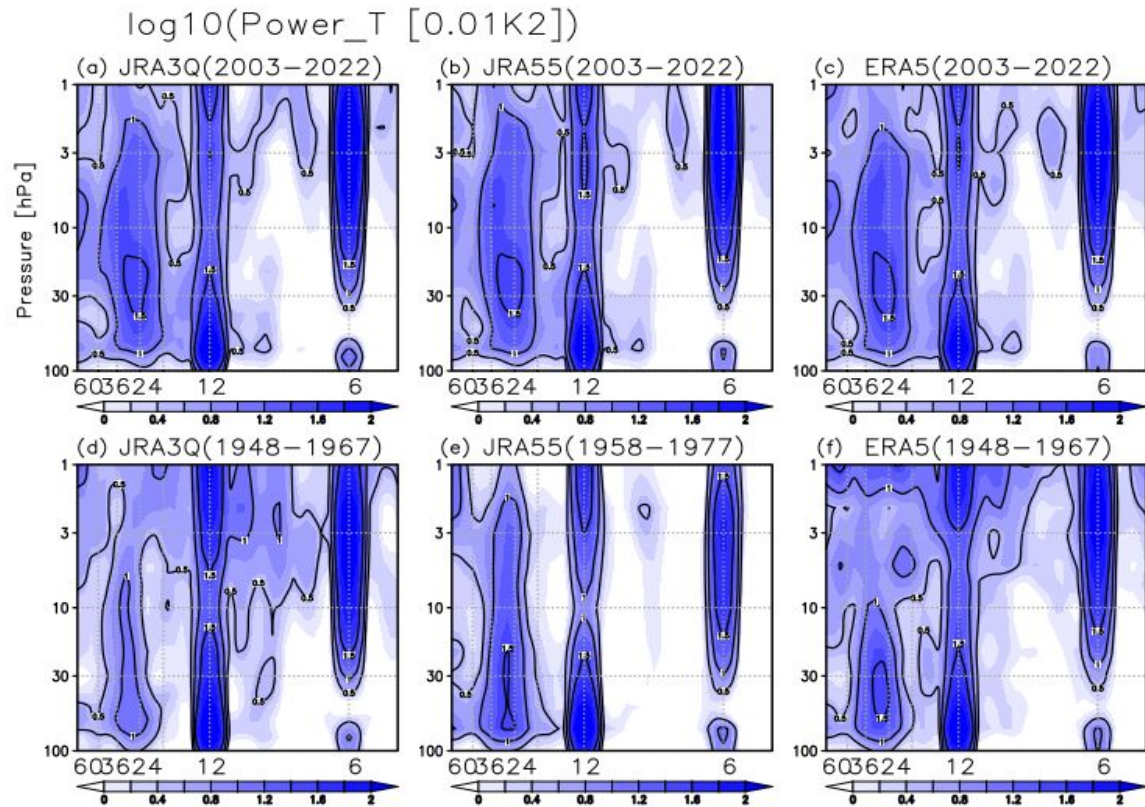
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1113 Fig. 13. Same as Fig. 12, but for QBO amplitude of temperature (K).

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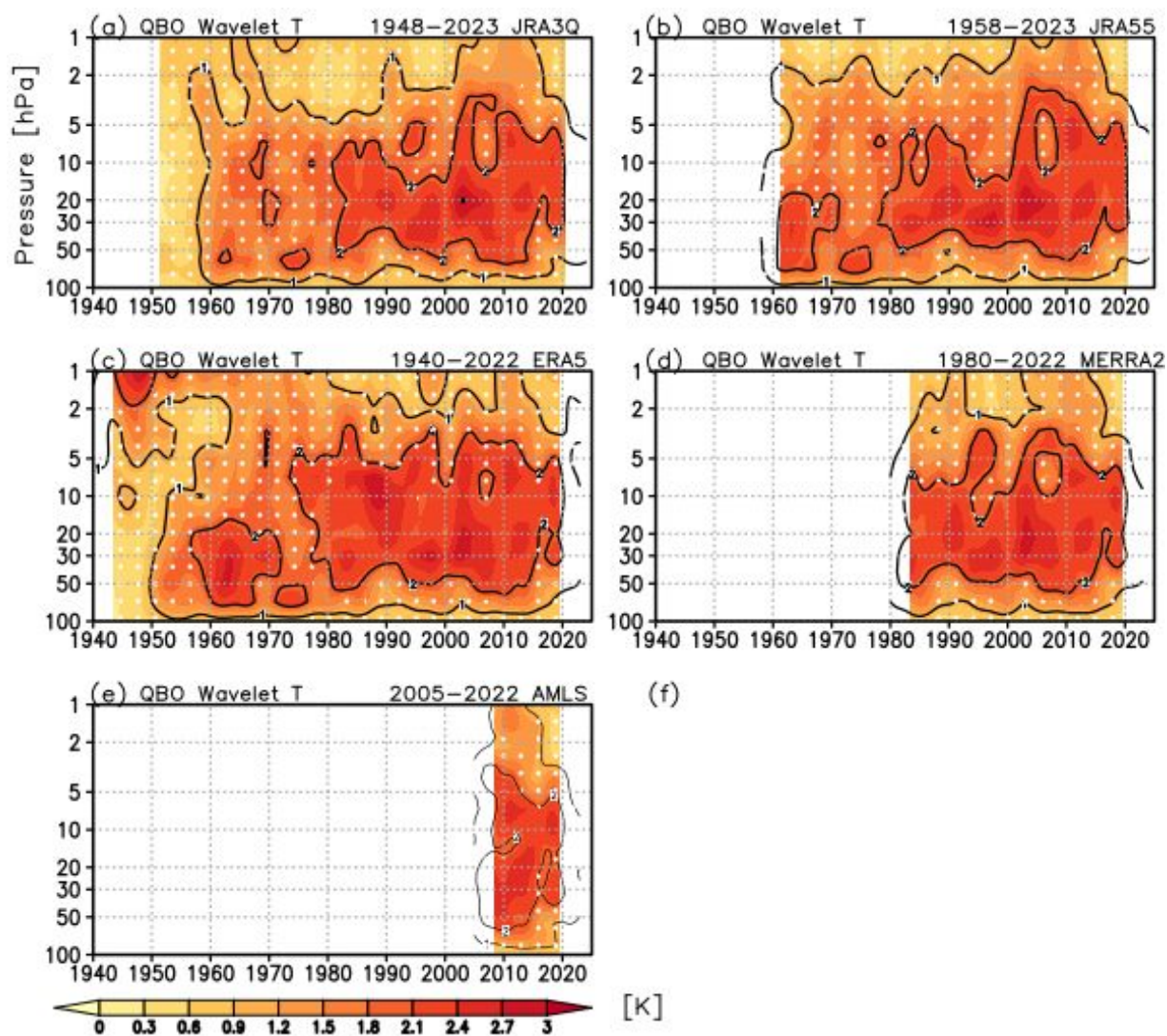
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1118 (Supplement figure)

1119 Fig. S1. Power spectra of zonal-mean temperature averaged over 10°S and 10°N from 100
 1120 hPa to 1 hPa during a post-satellite era 2003–2022 for (a) JRA-3Q, (b) MERRA-2, and (c)
 1121 ERA5. Power spectra during pre-satellite eras for (d) 1948–1967 JRA-3Q, (e) 1958–
 1122 1977 JRA-55 and (f) 1948–1967 ERA5. Values are shown on a logarithmic scale of base
 1123 10, and are expressed in units of K^2 . The contour interval is 0.4.

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1127 (Supplement figure)

1128 Fig. S2. Time series of wavelet power amplitude profile of temperature (K) for (a) JRA-3Q,
 1129 (b) JRA-55, (c) ERA5, (d) MERRA-2, and (e) AMLS. The QBO is defined in the wavelet
 1130 power spectrum from 20 to 40 months, with the power amplitude assumed to be square
 1131 root of twice the power. The dot indicates the confidence below the 95% level, based on
 1132 the background red noise taken from the post-satellite era from 1980 to 2022.